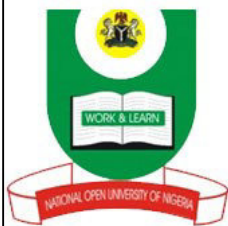


**COURSE  
GUIDE**

**ECO 454  
APPLIED ECONOMETRICS II**

**Course Team**      Dr Likita J. Ogba (Course Writer/Developer) -  
UNIJOS  
Dr. Adesina-Uthman, Ganiyat Adejoke, ACMA,  
FMNES, FCE (Course Editor) – NOUN



**NATIONAL OPEN UNIVERSITY OF NIGERIA**

© 2018 by NOUN Press  
National Open University of Nigeria  
Headquarters  
University Village  
Plot 91, Cadastral Zone  
Nnamdi Azikiwe Expressway  
Jabi, Abuja

Lagos Office  
14/16 Ahmadu Bello Way  
Victoria Island, Lagos

e-mail: [centralinfo@nou.edu.ng](mailto:centralinfo@nou.edu.ng)

URL: [www.nou.edu.ng](http://www.nou.edu.ng)

All rights reserved. No part of this book may be reproduced, in any form or by any means, without permission in writing from the publisher.

Printed 2018

ISBN: 978-978-8521-43-3

<b>CONTENTS</b>	<b>PAGE</b>
Introduction:.....	iv
What you will learn in this course:.....	iv
Course Contents:.....	v
Course Aims:.....	v
Course Objectives:.....	v
Working through the Course:.....	vi
Study Units:.....	vi
Assignment:.....	vi
Tutor Marked Assignments (TMAs):.....	viii
Final Written Examination:.....	viii
How to get the most from this course:.....	x
Conclusion:.....	xi

## **INTRODUCTION**

Welcome to ECO 454 Applied Econometrics II. The course is available for students in undergraduate Economics. The Course Applied Econometrics II

(ECO454) is a core course which carries two credit units. It is prepared and made available to all the students who are taking Economics; a programme tenable in the School of Arts and Social Sciences. The course provides an opportunity for students to acquire a detailed knowledge and understanding of theory and applications of econometrics in data for policy interpretations. The course is a useful material to in your academic pursuit as well as in your workplace as economists, managers and administrators.

This Course Guide is meant to provide you with the necessary information about the use of data run regression and provide policy interpretations. The course demonstrate the nature of the materials you will be using and how to make the best use of the materials towards ensuring adequate success in your programme as well as the practice of policy analysis. Also included in this course guide are information on how to make use of your time and information on how to tackle the tutor-marked assignment (TMA) questions. There will be tutorial sessions during which your instructional facilitator will take you through your difficult areas and at the same time have meaningful interaction with your fellow learners.

Overall, this module will fill an important niche in the study of applied economics which has been missing on the pathway of Economics Students will acquire an understanding of the method of practical data estimation and the skills to evaluate and discuss econometric literature.

## **WHAT YOU WILL LEARN IN THIS COURSE**

Applied Econometrics provides you with the opportunity to gain mastery and an in - depth understanding of application of economics quantitatively. If you devote yourself to practice of the software you will become used to quantitative analysis using different types of data. The data used will form part of the practical focus of real application implementation.

## **COURSE AIM**

This course will introduce you to the major aspects of applied econometrics.

This begins with knowing the basic assumptions of econometric variables that will be estimated. The practical estimation of models using real life data and identify deviations from models. The course will give you an opportunity to determine model variables stationarity and the use of other options in estimation of econometric models. In this course you will learn about advanced applications of econometrics and how to use such in policy analysis.

### **COURSE OBJECTIVES**

By the end of this course you should be able to

- Run a regression using a time series data
- Determine data stationary using Dickey Fuller method
- Evaluate the identification of an equation model
- Discuss simultaneous equation model
- Evaluate and discuss other methods of model estimation

### **WORKING THROUGH THE COURSE**

To complete this course you are required to read the study units, read the set text books and read other materials that would be provided to you by the National Open University of Nigeria (NOUN). You will also need to undertake practical exercise using Econometric Views (Eviews) software this require that you have access to personal computer, purchase and install Eviews for practical. Each unit contains self-assessment exercise; and at certain points during the course, you will

be expected to submit assignments. At the end of the course you will be expected to write a final examination. The course will take you about 12 weeks to complete.

Below are the components of the course. What you should do and how to allocate your time to each unit so as to complete the course successfully and on time.

### **COURSE MATERIALS**

Major components of the course are:

1. Course Guide
2. Study Units
3. Textbooks
4. Assignment Guide

## STUDY UNITS

There are twelve units in this course, which should be studied carefully. Such units are as follows:

### Module 1

Unit 1	Stages of Applied Econometric Research
Unit 2	Model Estimation
Unit 3	Statistical Test of Significance of OLS Estimates
Unit 4	Stationarity of Time series Data

### Module 2

Unit 1	General Forecasting
Unit 2	Forecasting and Seasonal Variation
Unit 3	Identification as an Econometric Problem
Unit 4	Two stage Least Square (2SLQ)

### Module 3

Unit 1	Simultaneous Equation
Unit 2	Instrumental Variable Method (IV)
Unit 3	Full Information Likelihood Method
Unit 4	Three Stage Least Square (3SLS)

## TEXTBOOKS AND REFERENCES

There are certain textbooks that have been recommended for this course. You should ensure that you read them where you are so directed before attempting the exercise.

## ASSIGNMENT

There are many assignments on this course and you are expected to do all of them by following the schedule prescribed for them in terms of when to attempt them and submit same for grading by your tutor. The marks you obtain for these assignments will count towards the final score.

## TUTOR-MARKED ASSIGNMENT

In doing the tutor-marked assignment, you are to apply your transfer knowledge and what you have learnt in the contents of the study units. These assignments which are many in number are expected to be turned

in to your Tutor for grading. They constitute 30% of the total score for the course.

## FINAL WRITTEN EXAMINATION

At the end of the course, you will write the final examination. It will attract the remaining 70%. This makes the total final score to be 100%.

## COURSE OVERVIEW

The table below brings together the units and the number of weeks you should take to complete them and the assignment that follow them.

Unit	Title of work	Weekly activity	Assignment (end of Unit)
1	Stages of Applied Econometric Research	1	1
2	Model Estimation	1	1
3	Statistical Test of Significance of OLS Estimates	1	1
4	Confidence interval of Econometric Estimates	1	1
5	Stationarity of Time Series Data	1	1
6	General Forecasting	1	1
7	Forecasting and Seasonal Variation	1	1
8	Identification as an Econometric Problem	1	1
9	Two Stage Least Square (2SLQ)	1	1
10	Simultaneous Equation	1	1
11	Instrumental Variable Method	1	1
12	Full Information Maximum likelihood Method	1	1
13	Three Stage Least Square (3SLS)	1	1

## HOW TO GET THE MOST FROM THIS COURSE

In distance learning, the study units replace the lecturer. There is the advantage of reading and working through the course material at the pace that suits the learner best. You are advised to think of it as reading the lecture as against listening to the lecturer. The study units provide exercises for you to do at appropriate periods instead of receiving exercises in the class.

Each unit has common features which are designed, purposely, to facilitate your reading. The first feature being an introduction to the unit, the manner in which each unit is integrated with other units and the entire course. The second feature is a set of learning objectives. These objectives should guide your study. After completing the unit, you should go back and check whether you have achieved the objectives or not. The next feature is self-assessment exercises, study questions which are found throughout each unit.

The exercises are designed basically to help you recall what you have studied and to assess your learning by yourself. You should do each self-assessment exercise and features are conclusion and summary at the end of each unit. These help you to recall all the main topics discussed in the main content of each unit. These are also tutor-marked assignments at the end of appropriate units. Working on these questions will help you to achieve the objectives of the unit and to prepare for the assignments which you will submit and the final examination.

It should take you a couple of hours to complete a study unit, including the exercises and assignments. Upon completion of the first unit, you are advised to note the length of time it took you, and then use this information to draw up a timetable to guide your study of the remaining units. The margins on either sides of each page are meant for you to make notes on main ideas or key points for your usage when revising the course. These features are for your usage to significantly increase your chances of passing the course.

## **FACILITATORS/TUTORS AND TUTORIALS**

There are 13 hours of tutorials provided in support of this course. You will be notified of the dates, times and location of these tutorials, together with the names and phone number of your tutor, as soon as you are allocated a tutorial group.

Your tutor will mark and comment on your assignments; keep a close watch on your progress and on any difficulties you may encounter as this will be of help to you during the course. You must mail your tutor-marked assignments to your tutor- well before the due date (at least two working days are required). They will be marked by your tutor and returned to you as soon as possible. Do not hesitate to contact your tutor by telephone, e-mail, or discussion board if you need help. The following may be circumstances in which you would find help necessary when:

- You do not understand any part of the study units or the assigned readings.



- You have difficulty with the self- assessment with your tutor's comment on an assignment or with the grading of an assignment.

You should try your best to attend tutorials. This is the only chance to have face-to-face contact with your tutor and to ask question which are course of your study. To gain maximum benefit from course tutorials, prepare your list of questions ahead of time. You will learn a lot from participating in the discussions.

## **CONCLUSION**

The course, Applied Econometrics (ECO454) exposes you to time series data utilization, model estimation and the issues involved in Applied Economics, such as the problem of simultaneous equation models, how to manage and solve them. On the successful completion of the course, you would have been armed with the materials necessary for efficient and effective management of applications of econometric related matters in any organization, policy institution and the country.

**MAIN  
COURSE**

<b>CONTENTS</b>	<b>PAGE</b>
<b>Module 1.....</b>	<b>1</b>
Unit 1      Stages of Applied Econometric Research	1
Unit 2      Model Estimation.....	11
Unit 3      Statistical Test of Significance of OLS Estimates .....	24
Unit 4      Stationarity of Time series Data.....	33
<b>Module 2.....</b>	<b>41</b>
Unit 1      General Forecasting.....	41
Unit 2      Forecasting and Seasonal Variation.....	54
Unit 3      Identification as an Econometric Problem	59
Unit 4      Two stage Least Square (2SLQ).....	65
<b>Module 3.....</b>	<b>71</b>
Unit 1      Simultaneous Equation.....	71
Unit 2      Instrumental Variable Method (IV) .....	80
Unit 3      Full Information Likelihood Method .....	85
Unit 4      Three Stage Least Square (3SLS).....	95

## **MODULE 1**

Unit 1 Stages of Applied Econometric Research

Unit 2 Model Estimation

Unit 3 Statistical Test of Significance of OLS Estimates

Unit 4 Confidence Interval of Econometric Estimates

Unit 5 Stationarity of Time series Data

### **UNIT 1 STAGES OF APPLIED ECONOMETRIC RESEARCH**

#### **CONTENTS**

1. INTRODUCTION
2. OBJECTIVES
- 3.0 MAIN CONTENT
  - 3.1 Stages of Applied Econometric Research.
  - 3.2 Concept of Economic and Econometric Model.
  - 3.3 Properties of a good Econometric Model.
- 4.0 CONCLUSION

- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

## **1.0 INTRODUCTION**

In econometric research there are different stages and one stage of the research leads to another, you need to learn these stages and know them in a chronological order. The stages of econometric research will help to give the basic foundational knowledge of what it takes to carry out an applied research. In this unit you will be exposed to the basic assumptions with respect to the independent variables to be estimated.

## **2.0 OBJECTIVES**

- Learn the basic stages of econometric research
- Learn the assumptions of econometric models

## **3.0 MAIN CONTENT**

### **3.1 STAGES OF APPLIED ECONOMETRIC RESEARCH**

In econometric research there are four main stages. These stages follow a chronological order, a good knowledge of economic theory will assist in identifying the econometric research structure and the characteristics associated with it, some of these basic stages of applied econometric research include:

**(i) Model Formulation:** This stage involves expressing economic relationships between the given variables in mathematical form. Here, one needs to determine the dependent variable as well as the explanatory variable(s) which will be included in the model. Also expressed here is a prior theoretical expectation regarding the sign and size of the parameters of the function, as well as the nature of the mathematical form the model will take such that the model is theoretically meaningful and mathematically useful.

Model specification or formulation therefore, presupposes knowledge of economic theory and the familiarity with the particular phenomenon under investigation, the theoretical knowledge allows the researcher to have an idea of the interdependence of the variables under study.

**(ii) Model Estimation:**

Model estimation entails obtaining numerical estimates (values) of the coefficients of the specified model by means of appropriate econometrics techniques. This gives the model a precise form with appropriate signs of the parameters for easy analysis. In estimating the specified model, the following steps are important.

- Data collection based on the variables included in the model.
- Examining the identification conditions of the model to ensure that the function that is being estimated is the real function in question.
- Examining aggregation problems of the function to avoid biased estimates.
- Ensuring that the explanatory variables are not collinear, the situation which always results in misleading results.

- Appropriate methods should be adopted on the basis of the specified model.

**(iii). Evaluation of Model Estimates:**

Evaluation entails assessing the results of the calculation in order to test their reliability. The results from the evaluation enable us to judge whether the estimates of the parameters are theoretically meaningful and statistically satisfactory for the econometric research.

**(iv). Testing the Forecasting Power of the Estimated Model**

Before the estimated model can be put to use, it is necessary to test its forecasting power. This will enable one to be assured on the stability of the estimates in term of their sensitivity to changes in the size of the model even outside the given sample data within the period.

**SELF ASSESSMENT EXERCISE**

Outline the basic stages of an econometric research

**3.2 CONCEPTS OF ECONOMIC AND ECONOMETRIC MODEL**

A model is a simplified representation of a real world process. That is, it is a prototype of reality, and so describes the way in which variables are interrelated.

These models exhibit the power of deductive reasoning in drawing conclusions relevant to economic policy.

Economic model describes the way in which economic variables are interrelated. Such model is built from the various relationships between the given variables.

In examining these concepts Bergstron (1966) defined model as any set of assumption and relationships which approximately describe the behaviour of an economy or a sector of an economy. In this way, an economic model guides economic analysis.

Econometric model on the other hand, consists of a system of equations which relate observable variables and unobservable random variables using a set of assumptions about the statistical properties of the random variables. In this respect, econometric model is built on the basis of economic theory.

Econometric model differs from economic model in the following ways:

- i. For an econometric model, its parameters can be estimated using appropriate econometric techniques.
- ii. In formulating econometric model, it is usually necessary to decide the variables to be included or not. Thus, the variables here are selective, depending on the available statistical data.
- iii. Because of the specific nature of econometric model, it allows fitting in line of best fit, and this is not possible with economic model.
- iv. The formulation of an econometric model involves the introduction of random disturbance term. This will enable random element that are not accounted for to be taken care of in the sample.

The “goodness” of an econometric model is judged on the basis of some basic fundamental properties that are universal in nature the following are some of these properties:

- i. *Conformity with economic theory.* A good model should agree with the postulate of economic theory. It should describe precisely the economic phenomena to which it relates.
- ii. *Accuracy* – the estimate of the co-efficient should be accurate. They should approximate as best as possible the true parameters of the structural model.
- iii. *The model should possess explanatory ability.* That is, it should be able to explain the observations of the real world. Example a model should explain price, demand, supply exchange rates, market behaviour, and any other practical situation.
- iv. *Prediction.* The model should be able to correctly predict future values of the dependent variable. Example a model should predict with accuracy price, demand, supply exchange rates, market behaviour, and any other practical situation. This feature often help strengthen the validity of an econometric model within a given period.
- v. *Mathematical form.* The mathematical form of the model should be simple with fewer equations. Such model should represent economic relationships with maximum simplicity.



- vi. *Identification.* The equations of the model should be easily identified that is, it must have a unique mathematical form. This means the model should either be exactly identified, over identified or under identified

## **SELF ASSESSMENT EXERCISE**

Discuss the properties of a good econometric model

### **4.0 CONCLUSION**

In this unit you have learn the basic stages of applied econometric research, these stages of econometric model research are necessary for effective analysis of any model building. You need to learn these steps well because their violation leads to several econometric problems that we shall study in this course.

### **5.0 SUMMARY**

In this unit you have learn the stages that could be followed in order to carry out acceptable and standard econometric model estimation. You have also learned the properties of econometric model estimation.

### **6.0 TUTOR MARKED ASSIGNMENT**

- 1 Discuss the various stages of an econometric research.
- 2 Carefully discuss the properties of an econometric model.

### **7.0 REFERNCES/ FURTHER READING**

Asteriou D and Hall S.G. (2007) Applied Econometrics: A Modern Approach using Eviews and Microfit. Macmillan pal Grave New York.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley,

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam,.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer, J. S. (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K..

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) Econometric Analysis, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) Introductory Econometrics, Harvard University Press.

Gujarati, D.N. (2003). Basic Econometrics. Tata Mc-Graw – Hill Publishing  
Company Ltd New-Delhi.

Koutsoyiannis, A. (1977) Theory of Econometrics An Introductory Exposition  
Econometric Methods Macmillan

Wooldridge, J. M. (2009) Introductory Econometrics A modern Approach, Cengage  
Learning Singapore 4<sup>th</sup> Edition

## **UNIT 2 SIMPLE LINEAR REGRESSION MODEL.**

### **CONTENTS**

- 1.0 INTRODUCTION
- 2.0 OBJECTIVES
- 3.0 MAIN CONTENT
  - 3.1 Parameter Estimation Strategies
    - 3.1.1 Sources of Deviations in Parameters and Models
    - 3.1.2 The uses of Random Variable in Models
  - 3.2 Assumptions of Linear Stochastic Regression Model
    - 3.2.1 Assumptions with respect to the random variable
    - 3.2.2 Assumption of error term with respect to the explanatory variable
    - 3.2.3 Assumption in Relation to the Explanatory Variable.
  - 3.3 Numerical Estimation of Parameters.
    - 3.3.1 Algebraic Method.
    - 3.3.2 Quantitative Method Illustration.
  - 3.4 Eviews Software Applications.
- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

### **INTRODUCTION**

Linear model shows the relationship between two variables. In this relationship, one variable is depending on the other variable. The model consists of the independent variables and the constant term, with their respective coefficient and we need to estimate the parameters of the model in order to know the magnitude of their relationship. Consider a familiar supply function of the form  $Y = b_0 + b_1X$  . . . . . (1). This function shows the positive linear relationship between quantity supply, Y and price of the commodity, X. The dependent variable in this model is the quantity supply, denoted by Y, while the independent variable (explanatory variable) is the price, X. This is a two variable case with two parameters representing the intercept and the slope of the function. This supply-price relationship,  $Y = f(x)$  is a one way causation between the variables Y and X: price is the cause of changes in the quantity supply, but not the other way round. From the above equation (. . . 1), the parameters are  $b_0$  and  $b_1$ , and we need to obtain numerical value of these parameters.

The left hand variable Y is variously referred to as the endogenous variables, the regressand, the dependent variable or the explained variable. Similarly, the right hand variable X is variously described as exogenous variables, the regressor, the independent variable or the explanatory variable.

## **2.0 OBJECTIVES**

At the end of this unit you should be able to:

- Discuss parameter estimation procedures.
- Discuss the assumptions of the stochastic variable.
- Discuss the assumptions of the explanatory variables.
- Attempt algebraic and software estimation of simple regression.

## **3.0 MAIN CONTENT**

### **3.1 PARAMETER ESTIMATION STRATEGIES**

The parameters of this model are to be estimated using ordinary least square (OLS) method. We shall employ this method for a start due to the following reasons.

- i. The computational procedure using this method is easy and straight forward.
- ii. The mechanics of the OLS. method are simple to understand.
- iii. This method always produces satisfactory results.
- iv. The parameter estimates using the O.L.S. method are best, Linear and unbiased. This makes the estimates to be more accurate compared with the estimates obtained using other method.
- v. The OLS. method is an essential component of most econometric techniques.

Note that the model  $Y = b_0 + b_1X$  implies an exact relationship between Y and X that is, all the variation in Y is due to changes in X only, and no other factor(s) responsible for the change. When this is represented on a graph, the pairs of observation (Y and X) would all lie on a straight line

Ideally, if we gather observations on the quantity actually supplied in the market at various prices and plot them on a diagram, we will notice that they do not really lie on a straight line.

#### **3.1.1 Sources of Deviations in Parameter Model Estimation**

There are deviations of observations from the line. These deviations are attributable to the following factors:

- *Omission of variable(s)* from the function on ground that some of these variables may not be known to be relevant.
- *Random behaviour of human beings.* Human reactions at times are unpredictable and may cause deviation from the normal behavioral pattern depicted by the line.
- *Imperfect specification of the mathematical form of the model.* A linear model, for instance, may mistakenly be formulated as a non-linear model. It is also possible that some equations might have been left out in the model.
- *Error of aggregation* – usually, in model specification, we use aggregate data in which we add magnitudes relating to individuals whose behaviour differs. The additions and approximations could lead to the existence of errors in econometric models.
- *Error of measurement* – this error arises in the course of data collection, especially in the methods used in the collection of data. Data on the same subject collected from central bank of Nigeria and National Bureau of statistics could vary in magnitude and units of measurements. Therefore when you use different sources you could get different results.

### **SELF ASSESSMENT EXERCISE**

In econometric analysis there are several sources of deviations from the actual model estimates discuss some of the sources of deviation.

#### **3.1.2 The Uses of Random variable in Models**

The inclusion of a random variable usually denoted by U, into the econometric function help in overcoming the above stated sources of errors. The U's is variously termed the error term, the random disturbance term, or the stochastic term.

This is so called because its introduction into the system disturbs the exact relationship which is assumed to exist between Y and the X. Thus, the variation in Y could be explained in terms of explanatory variable X and the random disturbance term U.

$$\text{That is } Y = b_0 + b_1X + u_i \dots\dots\dots (ii)$$

Where Y = variation in Y;  $b_0 + b_1X$  = systematic variation,  $U_i$  = random variation. Simply put, variation in Y = explained variation plus unexplained variation. Thus,  $Y = b_0 + b_1X + U_i$  is the true relationship that connects the variable Y and X and this is our regression model which we need to estimate its parameters using OLS method. To achieve this, we need observations on X, Y and U. However, U is not observed directly like any other variables, thus, the following assumptions hold:

### **3.2 ASSUMPTIONS OF THE LINEAR STOCHASTIC REGRESSION MODEL**

#### **3.2.1 Assumptions With Respect To Random Variable**

In respect to the random variable U, the following assumptions apply to any given econometric model that is used in prediction of any economic phenomenon:

- (i)  $U_i$  is a random variable, this means that the value which  $U_i$  takes in any one period depends on chance. Such values may be positive, negative or Zero. For

this assumption to hold, the omitted variables should be numerous and should change in different directions.

(ii) The mean value of “U” in any particular period is zero. That is,  $E(u_i)$  denoted by  $U$  is zero. By this assumption, we may express our regression in (ii) above as  $Y_i = b_0 + b_1x$ .

(iii) The variance of  $u_i$  is constant in each period. That is,

$$\text{Var}(u_i) = E(u_i)^2 = \delta(u_i)^2 = \delta^2u$$

which is constant. This implies that for all values of  $x$ , the  $U$ 's will show the same dispersion about their mean. Violation of this assumption makes the  $U$ s heteroscedastic.

(iv)  $U$  has a normal distribution. That is, a bell shaped symmetrical distribution about their zero mean. Thus,  $U = N(0, 1)$ .

(v) The covariance of  $u_i$  and  $u_j = 0$ .  $i \neq j$ . This assumes the absence of autocorrelation among the  $u_i$ . In this respect, the value of  $u$  in one period is not related to its value in another period.

#### SELF – ASSESSMENT EXERCISE

Discuss the assumptions with respect to the random variable

#### **3.2.2 Assumptions in terms of the relationship between ‘u’ and the explanatory variables.**



The following assumptions also hold when you conduct a regression analysis in terms of the relationship between the explanatory variable and the stochastic variable:

- i. U and X do not covary. This means that there is no correlation between the disturbance term and the explanatory variable. Therefore,  $\text{cov. } Xu = 0$ .
- ii. The explanatory variables are measured without error. This is because the U absorbs any error of omission in the model.

**3.2.3 Assumptions in relation to the explanatory variable(s) alone.** The following assumptions are made.

- (i) The explanatory variables are not linearly correlated. That is, there is absence of multicollinearity among the explanatory variables. This means that  $\text{cov. } X_i X_j = 0$ .  $i \neq j$  (This assumption applies to multiple regression model).
- (ii) The explanatory variables are correctly aggregated. It is assumed that the correct procedures for such aggregate explanatory variables are used.
- (iii) The coefficients of the relationships to be estimated are assumed to have a unique mathematical form. That is, the variables are easily identified.
- (iv) The relationships to be estimated are correctly specified.

### **SELF ASSESSMENT EXERCISE**

Discuss the assumptions of the random variable, the assumption of  $u$  with respect to the other explanatory variables.

### 3.3 NUMERICAL ESTIMATION OF PARAMETERS

The following procedures are used in finding numerical values of the parameters  $b_0$  and  $b_1$ .

From the true relationship

$$Y_i = b_0 + b_1 x + u, \dots (i)$$

and the estimated relationship

$$\hat{Y} = b_0 + b_1 x + e_i,$$

the residual

$$e_i = Y_i - \hat{Y} \dots (ii)$$

Squaring the residual and summing over  $n$ , gives:

$$\sum e_i^2 = \sum (Y_i - \hat{Y})^2 \text{ or } \sum (Y_i - \hat{b}_0 - \hat{b}_1 X)^2 \dots (iii)$$

5.0 The expression in (2) is to be minimized with respect to  $b_0$  and  $b_1$  respectively.

$$\text{Thus } \frac{\delta \sum e^2}{\delta \sum b_0} \sum (Y_i - b_0 - b_1 X) (-1) = 2 \sum [Y_i - b_0 - b_1 X]$$

$$\delta \sum b_0$$

$$\text{Thus } \frac{\delta \sum e^2}{\delta \sum b_1} = -2 \sum (Y_i - b_0 - b_1 X) X_i$$

$$\delta \sum b_1$$

Setting each of the partial derivatives to Zero, and dividing each term by -2 the OLS estimate of  $b_0$  and  $b_1$  could be written in the form:

$$\sum Y_i - b_0 N - b_1 \sum x_i = 0 \dots (V)$$

$$\sum YX_i - b_0 \sum X - b_1 \sum X_i^2 = 0 \dots\dots\dots (Vi)$$

From which

$$\sum Y_i = b_0 N + b_1 \sum X_i \dots\dots\dots (Vii)$$

$$\sum Y_i X_i = b_0 \sum X + b_1 \sum X_i^2 \dots\dots\dots (Viii)$$

The two equations (vii) and (viii) are the normal equation of the regression model.

Using Cramer's rule, the values of the parameters  $b_0$  and  $b_1$  are respectively:

$$b_0 = \frac{\sum Y \sum X^2 - \sum X \sum Y X}{N \sum X^2 - (\sum X)^2} \dots\dots(iX)$$

$$b_1 = \frac{\sum Y \sum X - \sum X \sum Y}{N \sum X^2 - (\sum X)^2} \dots\dots(X)$$

Using lower case letters (i.e. deviation of the observations from their means). It can be shown that:

$$b_0 = \bar{Y} - b_1 \bar{X} \dots\dots\dots (Xi)$$

$$b_1 = \frac{\sum XY}{\sum X^2} \dots\dots\dots (Xii)$$

### 3.3.2 Quantitative Method Illustration

#### Example 1

Given the following data on the supply of commodity W, find the estimated supply function (Table 1).

No	Yi (Quantity)	Xi (Price)
1	64	8
2	68	10
3	44	6
4	48	9
5	50	6
6	65	10
7	45	7
8	56	8

The given expression for  $b_0$  and  $b_1$  in  $ix$  and  $x$  as well as that of  $(x_1)$  and  $(x_{11})$  lead us to reproduce the above Table as seen in table 2.

**Table 2:** Worksheet for the estimation of the supply function for w.

	Y	X	X <sup>2</sup>	XY	Y=Y-Y	x=X-X	x <sup>2</sup>	Xy	Y	E	e <sup>2</sup>
1	64	8	64	572	9	0	0	0	55	9	81
2	68	10	100	680	13	2	4	26	64	4	16

3	44	6	36	264	-11	-2	4	22	46	-2	4
4	48	9	81	432	-7	1	1	-7	59	-11.5	132.25
5	50	6	36	300	-5	-2	4	10	46	4	16
6	65	10	100	650	10	2	4	20	64	4	16
7	45	7	49	315	-10	-1	1	10	50.5	-5.5	32.25
8	56	8	64	448	1	0	0	0	55	1	1
n	$\sum Y$	$\sum X$	$\sum X^2$	$\sum XY$	$\sum Y=0$	$\sum X=0$	$\sum X^2$	$\sum Y$		$\sum e = 0$	$\sum e^2 = 281.5$
= 8	= 440	= 64	= 530	= 3601			= 18	= 81			

Where  $e$  = residual,  $Y = b_0 + b_1x$

From the Table 2.

$$\bar{Y} = \sum y/n = 55. \quad X = \sum x/n = 8$$

Therefore, using upper case letters,

$$b_0 = \frac{440(530) - (64)(3601)}{8(530) - (64)^2} = 19$$

$$8(530) - (64)^2$$

$$b_1 = \frac{8(3601) - (64)(440)}{8(530) - (64)^2} = 4.5$$

$$8(530) - (64)^2$$

Similarly, using lower case letters.

$$b_1 = \frac{\sum XY}{\sum X^2} = \frac{81}{18} = 4.5$$

$$\sum X^2 = 18$$

$$\widehat{b_0} = \bar{Y} - \widehat{b_1}\bar{X} = 55 - 4.5(8) = 19$$

### 3.4 EViews SOFTWARE APPLICATIONS

The linear regression can be solved using the software package using the following steps. Create an excel worksheet type the data for quantity (QUA)) and price (PRI). Open your Eviews software, go to file, create worksheet, copy the data on excel worksheet paste it on the Eviews worksheet already created go to file, import data. Go to ‘Quick’ on the tool bar scroll to estimate equation and click on it a dialogue box opens, type the respective quantity and price click ok, the output is as follows:

Dependent Variable: QUA  
 Method: Least Squares  
 Date: 04/19/15 Time: 16:28  
 Sample: 2000 2007  
 Included observations: 8

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	19.00000	13.14075	1.445884	0.1983
PRI	4.500000	1.614460	2.787309	0.0317
R-squared	0.564241	Mean dependent var		55.00000
Adjusted R-squared	0.491615	S.D. dependent var		9.606545
S.E. of regression	6.849574	Akaike info criterion		6.898568
Sum squared resid	281.5000	Schwarz criterion		6.918428
Log likelihood	-25.59427	Hannan-Quinn criter.		6.764618
F-statistic	7.769094	Durbin-Watson stat		1.722913
Prob(F-statistic)	0.031690			

The software estimated model for the data can be presented in a line form as follows:  
 $Qua = 19 + 4.5Pri$ , Qua represent the quantity while Pri represent the price. This similar to the one computed using the manual method in the regression.

Note (i) only one of the two methods is to be used, and each gives the same result. (ii) unless specified, one is free to use any of the methods.

From the values of  $b_0$  and  $b_1$ , the estimated regression line or equation is got by substituting these values into  $Y = b_0 + b_1X$  and this gives  $Y = 19 + 4.5X$ . Thus, given the values of  $x_1$  ( $1 = 1, 2, \dots, N$ ), the estimated values of  $Y$  can be obtained using the regression equation.

From the estimated regression line, one can estimate **price elasticity**. Recall the estimated regression equation.  $Y = b_0 + b_1x_i$

This is also the equation of the line with intercept  $b_0$  and slope  $b_1$ . Note that  $b_1 = \delta Y / \delta X$ . Therefore, price elasticity =  $b_1 = X_i / Y_i$ .

Taking the mean of  $X_i$  and  $Y_i$ , we have average elasticity,  $e_p = b_1 \cdot X_i / Y_i$ . Therefore  $e_p = 4.5(8) / 55 = 0.65$ .

#### **4.0 CONCLUSION**

In this unit you have learn the basic stages of applied econometric research, the assumptions of econometric model estimation. You need to learn these assumptions well because their violation leads to several econometric problems that we shall study in this course such as simultaneous equation bias.

#### **5.0 SUMMARY**

In this unit you have learn the stages that could be followed in order to carry out acceptable and standard econometric model estimation. You have also learn how to conduct an econometric model estimation.

#### **6.0 TUTOR MARKED ASSIGNMENT**

Outline the basic assumptions of linear regression.

Given the following data estimate the multiple regression equation using Realgdp as dependent variable and Privcons or Govcons as independent variable.

Realgdp	Privcons	Govcons
31546.8	27463.8	6473.2
205222.1	28574.9	7584.3
199685.3	30411.4	8406.3
185598.1	35215.1	8889.2
183563	42858.7	8459.2
201036.3	49302.9	9363.2
205971.4	51537.5	9424.5
204806.5	75981.1	8064.4
219875.6	106678.6	11311
236729.6	128186.2	12443.7
267550	177234.6	13977.4
265379.1	206813.5	15904.8
271365.5	373526.7	33115.1
274833.3	502775.2	46796.5
275450.6	610340.2	169669.2
281407.4	1387445.6	242737.5
293745.4	2124271.4	280384.4
302022.5	2091069.1	377779
310890.1	2371328.2	393547.2

Estimate the regression equation and interpret your findings.

## **7.0 REFERNCES/ FURTHER READING**

Asteriou D and Hall S.G. (2007) Applied Econometrics: A Modern Approach using Eviews and Microfit. Macmillan pal Grave New York.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley,



Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam,.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer,J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K..

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) Econometric Analysis, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) Introductory Econometrics, Harvard University Press.

Gujarati, D.N. (2003). Basic Econometrics. Tata Mc-Graw – Hill Publishing Company Ltd New-Delhi.

Koutsoyiannis, A. (1977) Theory of Econometrics An Introductory Exposition

Econometric Methods Macmillan

Wooldridge, J. M. (2009) Introductory Econometrics A modern Approach, Cengage Learning Singapore 4<sup>th</sup> Edition

## **UNIT 3 STATISTICAL TESTS OF SIGNIFICANCE OF THE OLS ESTIMATES.**

- 1.0 INTRODUCTION
- 2.0 OBJECTIVES
- 3.0 MAIN CONTENT
  - 3.1  $R^2$  and the regression line
  - 3.2 Test of Significance using  $R^2$ ,
  - 3.3 Test of Significance using Z
  - 3.4 Test of Significance using T test
- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

### **1.0 INTRODUCTION**

After the estimation of the model in the previous section, we need to test the explanatory power or goodness of fit of the model, as well as the statistical reliability/significance at a given level in respect of  $b_i$ . There are a number of tests that are used to measure and evaluate the econometric efficacy of the estimated equation. In this unit you will be taken through the rudiments of test of statistical significance so as to be able to evaluate and use models.

### **2.0 OBJECTIVES**

At the end of this unit you should be able to conduct an:

- $R^2$  test
- Z test
- T test

We need to test the explanatory power or goodness of fit of the model, as well as the statistical reliability/significance at a given level in respect of  $b_i$ .

This is achieved using the following tests:

- i. Coefficient of determination,  $r^2$ ,
- ii. Standard error test
- iii. Z and  $t$ -statistic (test)

### 3.0 MAIN CONTENT

#### 3.1 $R^2$ and the Regression Line

The coefficient of determination,  $r^2$ , is used in determining goodness of fit of the regression line obtained using the OLS method. That is, it is used in testing the explanatory power of the linear regression of  $Y$  on  $X$ .

Thus, in order to determine the degree to which the explanatory variable is able to explain the variation in the dependent variable  $Y$ , the  $r^2$  provides a useful guide.

If we measure the dispersion of observations around the regression line some may be closer to the line while others may be far away from it. Our argument is that the **closer these observed values are to the line, the better the goodness of fit**. On the basis of this, we may turn out to state that a change in the dependent variable,  $Y$ , is explained by changes in the explanatory (independent) variable  $X$ . To know

precisely the extent to which the total variation in  $Y$  is explained by the independent variable,  $X$ , we compute the value of  $r^2$  as the ratio of explained variation to total variation. That is,  $r^2 = \text{Explained variation} / \text{Total variation} = \sum \hat{y}^2 / \sum y^2$

However, the coefficient of determination,  $r^2$  determines the proportion of the variation in  $Y$  which is explained by variation in  $X$ . If for instance,  $r^2 = 0.75$ , it means that 75% of the variation in  $Y$  is due to the variation in  $X$ , while 25% of the variation is explained by the disturbance term,  $u$ . Thus, the regression line gives a good fit to the observed data.

If, however,  $r^2 = 0.45$ , it means that only 45% of the variation in  $Y$  is as a result of variation in  $X$ , while 55% of the variation is due to the disturbance term. This is a poor indication and the regression line does not give a good fit to the observed data. Generally, if  $r^2$  is 0.5 and above, it shows a good fit while a value of  $r^2$  less than 0.5 shows a bad fit.

Note that the  $r^2$  is much of relevance when the estimated model is used for forecasting. Note also that the value of  $r^2 = 0$  signifies that the independent variable cannot explain any change in the dependent variable, hence variation in the independent variable has no effect on the dependent variable.

### **SELF ASSESSMENT EXERCISE**

1. Carefully discuss the econometric significance of the  $r^2$
2. Attempt a simple regression analysis and discuss the explanatory power of  $r^2$

### **3.2 STATISTICAL SIGNIFICANCE OF $b_i$ USING STANDARD ERROR TEST.**

To use this test, it is important to know the mean and variance of the parameter estimates  $\hat{b}_0$  and  $\hat{b}_1$ . It has been established that the mean and variance of  $\hat{b}_0$  and  $\hat{b}_1$  are respectively.

$$E(\hat{b}_0) = b_0 ; \text{Var } \hat{b}_0 = \mathbf{E}(\hat{\mathbf{b}}_0 - \mathbf{b}_0)^2 = \delta^2 \text{U} \sum x_i^2 / n \sum x_i^2$$

$$E(\hat{b}_1) = b_1 ; \text{Var } b_1 = E(\hat{b}_1 - b_1)^2 = \delta^2 \text{u} / \sum x_i^2$$

The standard error test enables us to determine the degree of confidence in the validity of the estimate that is, from the test, we are able to know whether the estimates  $b_0$  and  $b_1$  are significantly different from zero. The test is mainly useful when the purpose of the research is the explanatory (analysis) of economic phenomena and the estimation of reliable values.

We formally start by stating the null hypothesis,  $H_0: \hat{b}_i = 0$ ,

Against the alternative hypothesis  $H_1: \hat{b}_i \neq 0$

The standard error for the parameter estimates  $b_0$  and  $b_1$  are respectively computed as shown:

$$\text{i. } S(\hat{b}_0) = \sqrt{\text{var}(\hat{b}_0)} = \sqrt{\delta^2 \sum x_i^2 / n \sum x_i^2}$$

$$\text{But } \delta^2 \text{u} = Ee^2 / n - 2$$

$$S(\hat{b}_0) = (\sum e^2) \sum X^2 / (n - 2) n \sum X^2$$

$$\text{ii. } S(\hat{b}_1) = \sqrt{\text{Var } \hat{b}_1} = \sqrt{\delta^2 \text{u} / \sum x^2} = (\sum e^2) / n - 2 (\sum X^2)$$

When the numerical values for the  $s(\hat{b}_0)$  and  $s(\hat{b}_1)$  are each compared with the numerical values of  $\hat{b}_0$  and  $\hat{b}_1$  the following decision rules apply.

- (i) If  $S\hat{b}_1 < \hat{b}_1/2$ , we reject the null hypothesis and conclude that  $b_1$  is statistically significant.
- (ii) If on the other hand,  $S\hat{b}_1 > \hat{b}_1/2$  we accept the null hypothesis that the true population parameter  $b_1 = 0$ . This concludes that the estimate is not statistically significant. Therefore, change in  $X$  has no effect on the values of  $Y$ .

The acceptance of the null hypothesis has economic implication. Thus, the acceptance of the null hypothesis  $\hat{b}_1 = 0$  implies that the explanatory variable to which this estimate relates does not influence the dependent variable  $Y$ , and should not be included in the function. This situation renders the relationship between  $Y$  and  $X$ , hence the regression equation is parallel to axis of the explanatory variable  $X$  in the case,  $Y = b_0 + 0X_i$  or  $Y = b_0$ . The zero slope indicates that no relationship exist between  $Y$  and  $X$ .

Similarly, if the null hypothesis  $b_0 = 0$  is accepted, on the basis that  $s(\hat{b}_0) > \frac{1}{2}\hat{b}_0$ , it implies that the intercept of this regression line is zero. Therefore, the line passes through the origin. In this case, the relationship between  $Y$  and  $X$  will be  $Y = 0 + b_1 X_i$ , or  $Y = b_1 X$ . The two situations are diagrammatically presented as shown:

## **EXAMPLE II.**

Refer to the example 1 on the regression analysis, the  $r^2$  and the standard errors  $S(\hat{b}_0)$ ,  $s(\hat{b}_1)$  are as computed:

From the computed values of the Table.

$\sum XY = 81, \sum X^2 = 18 \sum Y^2 = 646, \sum e^2 = 281.5, n = 8; K = 2$  Where  $K =$  degrees of freedom.

$$R^2 = \frac{\sum (XY)^2}{\sum X^2 \sum Y^2} = \frac{6561}{11628} = 0.56$$

Hence, X is a fairly good predictor of Y about 56% of the variation in Y is explained by variation in the explanatory variable X, while 44% is due to disturbance term u. Thus, the regression line fairly gives a good fit to the observed data. On the statistical significance of the parameter estimate we compute:

$$S(\hat{b}_0) = \sqrt{\frac{\sum e^2 \sum x^2}{(n-2)n \sum x^2}}$$

$$= \sqrt{\frac{281.5(530)}{6(8)(18)}} = 13.14$$

$$S(\hat{b}_1) = \sqrt{\frac{\sum e^2}{(n-2)\sum x^2}}$$

$$= \sqrt{\frac{281.5}{(6)18}} = 1.61$$

Thus, the result of our regression may be presented formally as:

$$\hat{Y} = 19 + 4.5X$$

(13.14) (1.61),  $R^2 = 0.56$ ,  $n = 8$

From the above estimated result,

$$\hat{b}_0 = 19; \hat{b}_1 = 4.5; \quad S(\hat{b}_0) = 13.14; \quad S(\hat{b}_1) = 1.61$$

Therefore,  $\frac{1}{2} \hat{b}_0$  and we accept the null hypothesis that  $H_0: b_0 = 0$ .

This shows that  $\hat{b}_0$  is not statistically significant. Similarly  $s(\hat{b}_1) < \frac{1}{2}\hat{b}_1$  and we reject the null hypothesis. Thus, the estimate  $\hat{b}_1$  is statistically significant. Note: the acceptance and meaningful interpretation of any econometric result entails a combination of high  $r^2$  and low standard errors.

### 3.3 Z TEST OF STATISTICAL SIGNIFICANCE OF OLS ESTIMATES

The z test is employed when the sample size is sufficiently large (ie  $n \geq 30$ ). It could be applied whether the population variance is known or not. The z test is applied using the formula,  $Z_i^* = \hat{b}_i / s\hat{b}_i$  where the  $z^*$  is the calculated  $z_i$  which is compared with the z table ( theoretical value of  $z$  ) at a given level of significance, say 5%. If  $-z < z^* < +z$  at 0.025, we accept the null hypothesis that  $H_0: b_1 = 0$ ; and conclude that the estimate is not statistically significant. If however  $z^* > z$ , then we accept that  $H_1: \hat{b}_0 \neq 0$  and the estimate is statistically significant.

Consider an estimated function from a sample of 50 observations in the form  $\hat{Y} = 15 + 6.8X$ .

$$(2.8) \quad (1.05)$$

To conduct a z test for the estimates  $\hat{b}_0$ , and  $\hat{b}_1$  at 5% level of significance we proceed as follows:  $H_0 : \hat{b}_i = 0$  (Null hypothesis)



$H_1 : \hat{b}_i \neq 0$  (Alternative hypothesis)

$$Z^* = \hat{b}_0 / s(\hat{b}_0) = 15/2.8 = 5.36 \text{ ( for } b_0)$$

$$Z^* = \hat{b}_1 / s(\hat{b}_1) = 6.8 / 1.05 = 6.48 \text{ (for } b_1)$$

Z table at 5% level of significance = 1.96

IF  $\hat{b}_0$ ,  $Z^* > Z$  Table; for  $b_1$ ,  $Z_1^* > Z$  Table

Therefore, the null hypothesis is rejected, and concludes that estimates  $b_0$  and  $b_1$  are statistically significant at 0.05 level

### 3.4 T- TEST OF SIGNIFICANCE OF $b_i$

The students test is used when the sample size is small (ie  $n < 30$ ) provided that the population of the parameter follows a normal distribution. With this in view, and taking degrees of freedom into consideration, we need to compare this with the theoretical  $t$ , at given level of significance, say 5%.

Our null and alternative hypothesis are respectively formulated thus

$$H_0: b_i = 0$$

$$H_1: b_i \neq 0$$

Following a normal distribution, our  $t$  is computed as follows:

$$t = \hat{b}_i / s(\hat{b}_i)$$

As stated previously, the empirical  $t$  ( $t$ ) value is compared with the table  $t$  with  $n - k$  degrees of freedom, given a 5% level of significance.

**Decision rule:** if  $-t_{0.025}^* < t < t_{0.025}$  (with  $n - k$  degree of freedom), we accept the null hypothesis, and conclude that our estimate  $b_1$  is not statistically significant at 0.05 level of significance.

If however,  $t^* > + t_{0.025}$ , we reject the null hypothesis, and accept the alternative hypothesis. This concludes that the estimate  $b_1$  is statistically significant.

### Example

Given a sample size of  $n=18$ , the model was estimated to be:

$$\hat{Y} = 21 + 0.75 X$$

$$(10.2) (1.4)$$

We wish to test the reliability of the estimates  $\hat{b}_0$  and  $\hat{b}_1$  respectively. From the estimated model,

$$\hat{b}_0 = 21, S(\hat{b}_0) 10.2; \hat{b}_1 = 0.75. S(\hat{b}_1) = 1.4$$

$$\text{Therefore, } t^* = \hat{b}_0 / S(\hat{b}_0) = 21/10.2 = 2.06 \text{ (for } b_0)$$

$$T^* = \hat{b}_1 / S(\hat{b}_1) = 0.75 / 1.4 = 0.54 \text{ (for } b_1)$$

The critical values of  $t$  for  $(n - k)$  or  $18 - 2 = 16$  d.f. are:

$$-t_{0.025} = -2.12 \text{ and } +t = 2.12.$$

For the estimate  $\hat{b}_0$ , we can see that  $t^* < t$  we accept the null hypothesis and conclude that the estimate  $\hat{b}_0$  is not statistically significant.

In the case of the estimate  $\hat{b}_1$  since  $t^* < t$  we also accept the null hypothesis and conclude that  $b_1$  is not statistically significant at 5% significance level.

## 4.0 CONCLUSION

In this unit you have learn how to determine and interpret coefficient of multiple determination  $R^2$ , the  $Z$  test and the  $T$  test for evaluating an estimated model. Evaluating the model helps in the assessment of reliability, how the model estimates can be used for policy and applications.

## 5.0 SUMMARY

$R^2$ ,  $T$  and  $Z$  tests are important components of econometric test that are used in evaluating the strength of econometric variables. A good and continuous learning of these methods will enable you to conduct an effective and useful econometric research.

## 6.0 TUTOR MARKED ASSIGNMENT

Given a sample size of  $n=20$ , the model was estimated to be:

$$\hat{Y} = 48 + 0.55 X$$

(12.2) (0.4)

Test the reliability of the estimates  $\hat{b}_0$  and  $\hat{b}_1$  respectively.

## 7.0 REFERNCES/ FURTHER READING

Asteriou D and Hall S.G. (2007) Applied Econometrics: A Modern Approach using Eviews and Microfit. Macmillan pal Grave New York.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley,

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam,.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer,J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K..

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Gujarati, D.N. (2003). Basic Econometrics. Tata Mc-Graw – Hill Publishing Company Ltd New-Delhi.

Koutsoyiannis, A. (1977) Theory of Econometrics An Introductory Exposition

Econometric Methods Macmillan

Wooldridge, J. M. (2009) Introductory Econometrics A modern Approach, Cengage Learning Singapore 4<sup>th</sup> Edition.

## **UNIT 4 CONFIDENCE INTERVAL OF ECONOMETRIC ESTIMATES**

### **1.0 INTRODUCTION**

- 2.0 OBJECTIVES
- 3.0 MAIN CONTENT
  - 3.1 Confidence Intervals of Parameter Estimates
  - 3.2 Ordinary Least Square Estimators.
- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

## 1.0 INTRODUCTION

One of the basic requirements in carrying out a regression analysis is an understanding of the level of confidence at which model variables are estimated. It serves as a control in model estimation. It helps in the measurement and reporting of model variables that are estimated at any given point in time. This is a dynamic process requiring deliberate and purposeful actions in order to ensure model compliance between the theoretical and the empirical model.

## 2.0 OBJECTIVES

At the end of this unit you should be able to

Discuss and apply confidence interval for  $b_0$

Discuss and apply confidence interval for  $b_1$

Understand the goodness of Estimators

## 3.0 MAIN CONTENT

### 3.1 CONFIDENCE INTERVAL FOR THE PARAMETER ESTIMATES

The construction of confidence intervals for the estimates  $b_0$  and  $b_1$  enables us to state how close to these estimates the true parameter lies. It shows the limiting

values within which the true parameter is expected to lie within a certain degree of confidence.

In econometrics, we usually choose 95%. This implies that the confidence limit computed from a given sample would include from a population parameter in 95% of the cases. That is, we are 95% confident that our parameter estimates represents the true population parameter.

Using the z distribution, the 95% confidence interval for the parameters  $b_i$  is constructed as follows:

$$\hat{b}_i - 1.96 (S\hat{b}_i) < b_i < \hat{b}_i + 1.96 S(\hat{b}_i)$$

This means that the unknown population parameter  $b_i$  will lie within the limit 95 times out of 100.

Thus, from the previous regression equation

$$\hat{Y} = 19 + 4.5X$$

$$(13.14) (1.61)$$

and choosing 95% for the coefficient, our confidence interval for  $\hat{b}_0$  is  $\hat{b}_0 - 1.96 s(\hat{b}_0) < b_0 < \hat{b}_0 + 1.96 (S\hat{b}_0)$

$= 19 - 1.96 (13.14) < b_0 < 19 + 1.96 (13.14) = -6.75 < b_0 < 44.75$ . This implies that the true population parameter  $b_0$  will lie between 6.75 and 44.75 with a probability of 0.95.

Similarly, the confidence interval for  $b_1$  is constructed as shown:

$$\hat{b}_1 - 1.96 S(\hat{b}_1) < b_1 < \hat{b}_1 + 1.96 (s\hat{b}_1) = 4.5 + 1.96 (1.61) < 4.5 + 1.96(1.61) \\ = 1.34 < b_1 < 7.66.$$

We also conclude that the true population will lie between 1.34 and 7.66 with a probability of 0.95.

**3.1.1 Confidence interval for the t-statistic:** It is also constructed the same way as for the z distribution. The difference is that the t - distribution uses n - k degree of freedom. Thus, the 95% confidence interval for the parameter estimates  $b_1$  is constructed as follows;

$$b_1 - t_{0.025} S(\hat{b}_1) < \hat{b}_1 < \hat{b}_1 + t_{0.025} S(\hat{b}_1) \text{ with } n - k \text{ degrees of freedom.}$$

**Example:**

From a sample of 20, if the estimated model was  $\hat{Y} = 13.25 + 1.8X$

$$(6.04) \quad (0.35)$$

The 95% confidence interval for the parameter estimates is constructed as shown: df = 20 - 2 = 18.

$$\text{For } b_0: \hat{b}_0 - 2.101 (s\hat{b}_0) < b_0 < \hat{b}_0 + 2.101 (s\hat{b}_0) = 13.25 - 2.101 (6.04) < b_0 < 13.25 + 2.101 (6.04) = 0.560 < b_0 < 25.94.$$

This shows that the value of the true population parameter  $b_0$  (or the intercept) will lie between 0.56 and 25.96 with a probability of 0.95.

$$\text{Also, for } b_1: b_1 - 2.101 (S\hat{b}_1) < b_1 + 2.101 (s\hat{b}_1)$$

$$= 1.8 - 2.101 (0.35) < b_1 < 1.8 + 2.101 (0.35)$$

This implies that the value of true parameter  $b_1$  will lie between 1.095 and 2.535, given a probability of 0.95.

### SELF ASSESSMENT EXERCISE

A sample of 20 was take, if the estimated model was  $\hat{Y} = 17.20 + 2.81X$

$$(4.01) \quad (0.65)$$

Determine the confidence interval for the parameter estimates.

### 3.2 ORDINARY LEAST SQUARE ESTIMATORS

The ordinary least square (OLS) is among the best method used in obtaining estimates of the parameter  $\hat{b}_i$  and  $\hat{b}_0$ . The use of OLS method in estimating economic relationship is based on the fact that the estimates of the parameters have some optimal properties.

Generally, in choosing a particular estimation method, one should aim at such method that gives an estimate, which is close to the value of the true population parameter; the variation of which (if at all it exists) will be within only a small range around the true parameter.

For any estimation method, the goodness of the estimator is judged on the basis of the following desirable properties.

- (i) **Unbiasedness:** - An estimator is unbiased if its mean is zero i.e.  $E(\hat{b}_i) - b_1 = 0$ . In such case, the unbiased estimator changes to the true value of the parameter as the number of samples increases. An unbiased estimator always



gives, on the average, the true value of the parameter. The cases of biased and unbiased estimator of the true value are as illustrated diagrammatically.

(ii) **Minimum Variance** – An estimator is best if it has the smallest variance compared with any other estimate obtained using other methods. By minimum variance, we mean that the values of the parameter  $b_i$  clusters very closely around the true parameter  $b$ , as seen in the diagram:

In the diagrams, (B) is the best compared with (A) because (B) has minimum variance as seen in the narrowness of the distribution.

(iii) **Efficient estimator:** An estimator is efficient when it combines the property of unbiasedness with minimum variance property.

Symbolically  $b_i$  is efficient if the following two conditions are fulfilled.

$$(a) \quad E(b) = b: \quad (b) \quad E[\hat{b} - E(\hat{b})]^2 < E(b^*)^2$$

Where  $b^*$  is another unbiased estimate of the true  $b$ . This means that in the class of unbiased estimators, such estimator has a minimum variance.

(iv) **Linear Estimator:** An estimator is linear if it is a linear combination of the given sample data. Thus, with the sample observation  $Y_1, Y_2, \dots, Y_n$ , a linear estimator takes the form:

$$K_1Y_1 + K_2Y_2 + \dots + K_nY_n, \text{ where the } k_i \text{ s are some constants.}$$

(v) **BLUE (Best, Linear, Unbiased, Estimator)**

This property is abbreviated to BLUE meaning that the estimator is best (having minimum variance) linear, and unbiased as compared with all other linear unbiased estimators.

Thus all the properties (i-iv) are included in the BLUE property.

**(vi) Minimum mean square error (MSE) Estimators.**

This property combines unbiasedness and the minimum variance properties. An estimator, therefore, is a minimum MSE estimator if it has the smallest mean square error, defined as the expected value of the squared difference of the estimator around the true population parameter  $b$ . that is,  $MSE(\hat{b}) = (\hat{b} - b)^2$

**(viii) Sufficiency:**

This property implies that the estimator uses all the available information a sample contains about the true parameter. For this property to hold, the estimator should accommodate all the observations of the sample, and should not give room for any additional information in connection with the true population parameter.

The ordinary least square method (OLS) satisfies the above stated properties. For this reason, the method seems to be the best and most widely used of all the estimation methods. In a nut shell, the OLS has the BLUE (best, linear, unbiased properties among the class of linear and unbiased estimators). The linearity property as previously discussed implies that the parameter estimates are linear functions of the observed  $Y_i$ . That is, the estimators  $b_0$  and  $b_1$  includes the variable  $Y$  and  $X$  in the first power.

Thus,  $\hat{b}_1 = f(Y)$ . This property enables one to compute the values of the parameter estimates with ease.

The unbiased property of the OLS estimates implies that the expected value of the estimates parameter is equal to the true value of the parameter, that is,  $E(\hat{b}_i) = b$ .

The importance of this property lies in the fact that for large samples, the parameter estimates obtained will on the average give a true value of the  $b$ 's.

The minimum variance property becomes desirable when combined with unbiasedness. The importance of this property is obvious when we want to apply the standard tests of significance for  $b_0$  and  $b_i$ , and to construct confidence intervals for these estimates. Because of the minimum variance they have, their respective confidence intervals will be narrower than for other estimates obtained using any other econometric procedures.

The smaller confidence interval obtained is interpreted to mean in effect that we are extracting more information from our sample than we would be, if we were to use any other methods which yielded the same unbiased estimates.

### **SELF ASSESSMENT EXERCISE**

- 1) Examine the properties of estimators in econometrics.
- 2) A sample of 32 was taken, if the estimated model was  $\hat{y} = 15.20 + 0.81X$   
(3.01) (0.60)

Determine the confidence interval for the parameter estimates.

### **4.0 CONCLUSION**

In this unit you have learn how to calculate confidence interval of the parameter estimates of models. This can be applied to model interpretation and the implication for the purpose of determining the use of the model.

### **5.0 SUMMARY**

Confidence interval of estimate and estimators of parameters are two basic requirements that are considered in the analysis of models in econometrics. Your ability to assess a model will depend on a combination of these econometric tests

## **6.0 TUTOR MARKED ASSIGNMENT**

1. Discuss the properties of ordinary least square estimators
2. A sample of 40 was taken, if the estimated model was  $\hat{Y} = 19.20 + 1.81X$

$$(2.01) \quad (0.25)$$

Determine the confidence interval for the parameter estimates.

## **7.0 REFERENCES/ FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.,

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley,

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam,.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer, J. S. (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K..

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) Econometric Analysis, 4<sup>th</sup> ed., Prentice Hall, Englewood cliffs, N. J.

Goldberger, Arthur S. (1998) Introductory Econometrics, Harvard University Press.

Harvey, A.C.( 1990) The Econometrics Analysis of Time Series, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) Econometric Methods, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) Undergraduate Econometrics, John Wiley & Sons, New York,.

Hu, The-Wei (1973) Econometrics: An Introductory Analysis, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee (1982) Introduction to the theory and practice of Econometrics, John Wiley & Sons, New York.

Katz, David A. (1962) Econometric Theory and Applications, Prentice Hall, Englewood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) Textbook of Econometrics, 2d ed., Prentice Hall, Englewood Cliffs, N.J.

Kmenta, Jan (1986) Elements of Econometrics, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) Introduction to Econometrics, John Wiley & Sons, 3d ed., New York,.

Mark, Stewart B., and Kenneth F. Wallis (1981) Introductory Econometrics, 2d ed., John Wiley & Sons, New York, . A Halsted Press Book.

Madansky, A. (1976) Foundations of Econometrics, 2d ed., North-Holland, Amsterdam.

Mills, T.C. (1993) The Econometric Modelling of Financial Time Series, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) *An Introduction to Applied Econometrics: A Time series Approach*, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) *Applied Econometrics*, Wadsworth, Belmont, California.

Theil, Henry (1971) *Principles of Econometrics*, John Wiley & Sons, New York.

Tintner, Gerhard (1965) *Econometrics*, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) *An Introduction to Econometrics*, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) *Econometrics*, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) *Introductory Econometrics*, South-Western College Publishing.

## **UNIT 5 STATIONARITY AND TIME SERIES DATA**

### **1. INTRODUCTION**

- 2. OBJECTIVES
- 6.0 MAIN CONTENT
  - 3.1 Meaning of Stationarity
  - 3.2 Test for stationarity
  - 3.3 Overcoming Non-Stationary data problem
  - 3.4 Econometric Applications
- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

## **1.0 INTRODUCTION**

Stationarity of data is considered to be most important and most effective aspect of data management in order to minimize the occurrence of spurious results in econometric model estimation. Stationarity is fundamental to all Modern Econometric Estimation.

## **2.0 OBJECTIVES**

At the end of this unit, you should be able to

- Define stationarity
- State the steps for determining stationarity in data management
- Determine and discuss data stationarity using Dickey Fuller method.

## **3.0 MAIN CONTENT**

### **3.1 MEANING OF STATIONARITY**



In econometric analysis, data is stationary when its means and variance are constant over time and the value of the covariance between the two time periods depends only on the distance or gap or lag between the two time periods and not the actual time at which the covariance is computed. (Gyujarati, 2005). Generally, if a time series data is stationary, its mean, variance and auto covariance at various lags remain the same no matter at what point they are measured, that is they are time invariant. The time series data will trend to return to its mean this is called mean reversion. The fluctuations around this mean measured by its variance will have a constant.

According to Woodridge (2009) a stationary time series processes one whose probability distribution are stable over time. In a collection of random variables in the sequence and then shift that sequence ahead some given time periods, the joint probability distribution should remain unchanged. However, it does not require that the nature of any correlation between adjacent terms is the same across all time periods.

Generally, a key concept underlying time series processes is that of stationarity. A time series is covariance stationary when it has the following three key characteristics:

- a) A stationary time series exhibits mean reversion in that fluctuates around a constant long run mean  $E(Y_t) = \text{constant}$  for all  $t$
- b) A stationary time series data has a finite variance that is time-invariant.  
 $Var(Y_t) = \text{constant}$  for all  $t$
- c) A stationary time series data has a theoretical correlogram that diminishes as the lag length increases.  $Cov(Y_t, Y_{t+k}) = \text{constant}$  for all  $t$  and  $k \neq 0$ .

Stationarity is important because if the series is non-stationary then all the typical result of the classical regression analysis is not valid. Regression with non-stationary series may have no meaning and are therefore called spurious.

It is also important to note that in stationary data shocks to such time series are necessarily temporary overtime. The effects of shocks will dissipate and the series will revert to its long run mean level. As such long-term forecast of a stationary series will converge to the unconditional mean of the series on the other hand non-stationary time series will necessarily contain permanent components so the mean and variance of non-stationary series will depend on time, which leads to case where a series has no long-run mean to which the series returns and the variance will depend on time and will approach infinity as time goes to infinity (Asteriou and Hall, 2007).

### **3.2 TEST FOR STATIONARITY**

There are several tests of stationarity but the most commonly used in applied econometrics is the Dickey – fuller augmented unit root test.

$$Y_t = \rho Y_{t-1} + \mu_t \quad -1 \leq \rho \leq 1 \quad \text{--- (1)}$$

Where  $\mu_t$  is a white noise error terms if  $\rho = 1$  in the case of unit root becomes a random walk model without drift which we know is a nonstationary stochastic process.

Using theoretic underpinning subtract  $Y_{t-1}$  on both side of equation (1)

$$Y_t - Y_{t-1} = \rho Y_t - Y_{t-1} + \mu_t \quad \text{--- (2)}$$

$$= (\rho - 1)Y_{t-1} + \mu_t \quad \text{--- (3)}$$

Equation 3 can be written alternatively as

$$\Delta Y_t = \sigma Y_{t-1} + \mu_t \quad \text{--- (4)}$$

Where  $\sigma = (1 - \rho)$  and  $\Delta$  is the first difference operator. Equation (4) is what is estimated and test the null hypothesis that  $\sigma = 0$  if  $\sigma = 0$ , then  $\rho = 1$  that is there is unit roots, meaning the time series is nonstationary.

Similarly, when  $\sigma = 0$  equation (4) becomes

$$\Delta Y_t = (Y_t - Y_{t-1}) = \mu_t \quad \text{--- (5)}$$

Since  $\mu_t$  is a white noise error term, it is stationary which means that the first difference of a random walk time series are stationary. In Estimation the first differences of  $Y_t$  and regress them on  $Y_{t-1}$  to see if the estimated slope coefficient in the regression ( $= \delta$ ) is zero or not. If it is zero, it shows that  $Y_t$  is nonstationary. But if it is negative we can conclude that  $Y_t$  is stationary.

### **3.2.1 Dickey Fuller Test**

The Dickey fuller test evaluates the null – hypothesis that  $\sigma = 0$  that is there is a unit root, meaning that the time series is nonstationary. The alternative hypothesis is that  $\sigma$  is less than zero that is the time series is stationary. When the null hypothesis is rejected, it means that  $Y_t$  is a stationary time series.

Applications: Using the following time series data determine the stationarity.

### **3.2.2 Transforming Nonstationary Time Series**

When data is tested for stationarity and they show nonstationarity, then do transform the nonstationary time series to make them stationary.

The process of transformation varies depending on whether the time series are difference stationary or trend stationary.

In differences stationarity it involves taking the first difference of the time series in order to make them stationary.

Similarly, if the time series are trend non stationary then we take the trend.

### 3.2.3 ECONOMETRIC APPLICATIONS.

Given the following data determine the stationarity using Dickey Fuller method.

Varasset	Fixasset
3820.1	1318.42
3757.9	1418.9
5382.8	1147.74
5949.5	1408.06
8418.3	1585.88
8804	1640.44
9313.8	1703.82
9993.6	1844.39
11339.2	2045.32
10899.6	2239.51
104368.1	4974.5
12243.8	5499.78
20512.7	6339.28
66787	7243.61
70714.6	8096.27
119391.6	112408.1
122800.9	157477.9
128331.8	158998.9
152409.6	162423
154188.6	162458.2
157835.4	162531.5
162343.4	182541.2
168831.6	182637
178478	183418.3
249229.6	184946.5
269844.7	188468.6
302848.3	189312.6

317571.2	188183.9
329381	187706.9
380339.7	191203.2
438201.3	194322.2

The procedure is as follows, open Eviews software create a worksheet, import your set of data by browsing and clicking to upload your data to the workbook; go to quick icon on the software toolbar select unit root a dialogue box opens input the variable name select Dickey Fuller unit root test click ok.

Null Hypothesis: VARASSET has a unit root  
 Exogenous: Constant  
 Lag Length: 1 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-0.055931	0.9413
Test critical values:		
1% level	-3.831511	
5% level	-3.029970	
10% level	-2.655194	

\*MacKinnon (1996) one-sided p-values.  
 Warning: Probabilities and critical values calculated for 20 observations and may not be accurate for a sample size of 19  
 Varasst is stationary because it satisfy the condition for stationarity based on the conditions stated in the unit

Null Hypothesis: FIXASSET has a unit root  
 Exogenous: Constant  
 Lag Length: 0 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	0.037045	0.9516
Test critical values:		
1% level	-3.808546	
5% level	-3.020686	
10% level	-2.650413	

\*MacKinnon (1996) one-sided p-values.  
 Fixasst is not stationary because it failed to meet the stationarity condition we therefore repeat the procedure and select level in the Dickey Fuller dialogue box. It can be concluded that it is stationary at level.

Null Hypothesis: D(FIXASSET) has a unit root  
 Exogenous: Constant  
 Lag Length: 0 (Automatic - based on SIC, maxlag=4)

	t-Statistic	Prob.*
--	-------------	--------

Augmented Dickey-Fuller test statistic		-3.016642	0.0513
Test critical values:	1% level	-3.831511	
	5% level	-3.029970	
	10% level	-2.655194	

\*MacKinnon (1996) one-sided p-values.

Warning: Probabilities and critical values calculated for 20 observations and may not be accurate for a sample size of 19

## 4.0 CONCLUSION

Stationarity of time series data is very important. If it is effectively achieved then the regression result will not be spurious. The result emerging after stationary test has been carried out can be used for policy analysis.

## 5.0 SUMMARY

In this unit, you have been taken through the process of knowing stationarity in econometrics you have also learnt about how to achieve stationarity in data management in econometric analysis.

## 6.0 TUTOR MARKED ASSIGNMENT

Given the following data test for the stationarity of gdpl and reerl using your Eviews software.

Gdpl	Reerl
11.83957	2.075806
11.78133	2.055386
11.75842	2.03529
11.73871	2.018888
11.71619	2.011659
11.73485	2.022474

11.88075	2.037689
11.9649	2.042883
12.00148	2.033174
12.00353	2.023693
12.09498	2.038501
12.09484	2.039128
12.13759	2.045691
12.11095	2.050573
12.13491	2.049547
12.19589	2.060913
12.19689	2.059162
12.15363	2.036549
12.16782	2.037144
12.16359	2.02435
12.12319	2.033106
12.12703	1.998442
12.16356	2.005447
12.25528	2.028002
12.31416	2.035662
12.33174	2
12.35529	2.031445
12.41397	2.03442
12.45549	2.04023
12.42315	2.040994

## **7.0 REFERENCES/FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.,

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley,

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam,.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.



Christ, C.F. ( 1966) *Econometric Models and Methods*, John Wiley & Sons, New York.

Cramer, J. S. (1969) *Empirical Econometric*, North-Holland, Amsterdam.

Davidson, James (2000). *Econometric Theory*, Blackwell Publishers, Oxford, U.K..

Desail, Meghnad. (1969) *Applied Econometrics*, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) *Introductory Econometrics*, Springer-Verlag, New York

Dutta, M. (1975) *Econometric Methods*, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) *Econometric Analysis*, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) *Introductory Econometrics*, Harvard University Press.

Harvey, A.C.( 1990) *The Econometrics Analysis of Time Series*, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York,.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee (1982) *Introduction to the theory and practice of Econometrics*, John Wiley & Sons, New York.

Katz, David A. (1962) *Econometric Theory and Applications*, Prentice Hall, Engle-wood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) *Textbook of Econometrics*, 2d ed., Prentice Hall, Engle-wood Cliffs, N.J.

Kmenta, Jan (1986) *Elements of Econometrics*, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) *Introduction to Econometrics*, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) *Introductory Econometrics*, 2d ed., John Wiley & Sons, New York, A Halsted Press Book.

Madansky, A. (1976) *Foundations of Econometrics*, 2d ed., North-Holland, Amsterdam.

Mills, T.C. (1993) *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) An Introduction to Applied Econometrics: A Time series Approach, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) Applied Econometrics, Wadsworth, Belmont, California.

Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) Econometrics, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

## **Module 2**

### Unit 1 General Forecasting

Unit 2 Forecasting and Seasonal Variation

Unit 3 Identification as an Econometric Problem

Unit 4 Two stage Least Square (2SLQ)

## **UNIT 1 GENERAL FORECASTING**

### **CONTENTS**

- 1.0 INTRODUCTION
- 2.0 OBJECTIVES
- 3.0 MAIN CONTENT
  - 3.1 Meaning of Forecasting
  - 3.2 Forecasting process linked period
  - 3.3 Moving average in forecasting
- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR-MARKET ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

### **1.0 INTRODUCTION**

Forecasting is often seen as bridge between the present economic events occurring and the future, it is needed for effective planning and future projections based on the present economic phenomenon. Forecasting is particularly important because resources are scarce coupled with the environmental uncertainties. It is therefore good to forecast and minimize the degree of uncertainty in the economy.

## **2.0 OBJECTIVES**

At the end of this unit you should be able to:

- Explain the meaning of forecasting
- Discuss moving average seasonal variations

## **3.0 MAIN CONTENT**

### **3.1 MEANING OF FORECASTING**

Forecasting is generally concerned with data associated with a time period of less than one year (i.e. calendar months, accounting periods in a year — usually 12 or 13, quarters, weeks, etc.); situations where forecasts are associated with a particular item and for which forecasts are updated every time period; situations where forecasts are required for a large number of items; situations where the forecasts produced for a particular item or product and are used on a period to period basis to:

- (a) Analyse demand and to assess appropriate inventory levels and production schedules, and
- (b) Analyse sales to help assess cash flows and to ascertain marketing procedures.

It is apparent that for these types of application the most appropriate forecasting model (or series of models) needs to be:

- (i) cheap to operate - in terms of implementation, routine updating and storage requirement costs;
- (ii) flexible and hence able to offer a variety of different, but closely related, model types suitable for a wide variety of items and situations for which forecasts could be required;
- (iii) largely automatic, such that a minimum of manual interruption is necessary;
- (iv) Well proven, and hence, readily available in both the literature and computer software.

The range of forecasting models based on the exponentially weighted average (collectively referred to as exponential smoothing methods), which were introduced in the early 1960's, has been shown to fulfill most of the above requirements.

The superiority of exponential smoothing methods over the traditional moving average concept is such that today most manufacturing organizations of any size use them and no industrial or business computer software is complete without them.

A stationary situation is one in which, although observed values fluctuate from one time period to the next, the average value remains steady over a reasonably long period of time. To illustrate this, this, a series of demand values plotted against time. It can be seen that the average value per month over the one-year period is

about 100 items per month, and that this average figure is neither increasing nor declining significantly with time. This is a typical stationary situation, with individual values fluctuating above and below a reasonably steady average

Examining non stationary situation however, reveals a completely different situation. Here the average value is definitely not stationary but increasing with time. Such a situation could arise with a product maintaining its share of a rapidly expanding market or a product gaining an increasing share of a static (or even declining) market. Exactly the types of market condition that cause such values can only be identified by sales and marketing intelligence, but whatever the reason, this forecasting situation is obviously a more complicated one than the stationary.

Before discussing the mathematical techniques involved in forecasting, it might be the best to discuss initially just what one should expect of forecasting system. First, it should be appreciated that because one's forecasts are based on past information, there will always be some degree of forecasting error. Accepting this, it is apparent that the most logical aim of a forecasting system should be to minimize such errors over a longish period of time. Because forecasting errors can be both positive and negative (i.e. the forecast can be below or above the actual value that occurs) a simple cumulative sum of the errors alone will not be a good indication of whether forecasting errors are being minimized or not, as this sum will tend towards zero

irrespective of the forecasting system used. A more effective measure is the cumulative sum of the squared errors since squaring always produces a positive result irrespective of whether the original figure was positive or negative. Thus all errors contribute towards the cumulative sum of squared errors.

Once it has been accepted that some degree of error is present in any forecasting system, it is evident that the forecast can be only an average value of what is expected to occur, with errors distributed evenly either side of that average. In practice it is generally assumed that these errors are distributed according to a probability distribution known as the Gaussian or Normal distribution. This point will not be explained further here except to say that the assumption is reasonably true so long as the value of the average per time period is not too low, which is generally true of the items we are concerned with in short-term forecasting if this average value is generally greater than ten.

Assuming that errors are distributed normally, we need some measure of the spread or the degree of dispersion of errors around the average. The usual measure of dispersion is known as the **standard deviation**, represented universally by the Greek **symbol  $\sigma$** , indicates a situation in which the standard deviation suddenly increases owing to a change in the underlying data pattern.



For this situation the forecast would not change appreciably as the average value remains at approximately 75 per month, even after the change. However, it is evident that the spread of values, or variation, has changed after the sixth month and this change, in an efficient forecasting system, would be noted by a change in the value of the standard deviation.

Thus there are two basic parameters we wish to estimate in any forecasting system. The **first is the actual forecast** which predicts what the expected or average value in the future is likely to be. The **second is the standard deviation** which measures the spread in dispersion of Individual values about that average.

### **Forecasting link- period**

A short-term forecasting system treats the total of individual values in each time period as a single item of data, i.e. demand per day, sales per week, production per month, etc. Increasing the length of the time period increases the sample size and hence reduces the variability of successive individual values per period thus enabling more accurate forecasts to be made. At the same time, however, the speed of response of the forecasting system to real or actual changes in the data is obviously reduced with longer time periods. A balance between these two effects can be achieved only by the selection of a suitable forecast time period.

It can be shown that the minimum value of the forecast time period should be of a duration to ensure that at least one non-zero value occurs in two time periods, that is that there is a 50 per cent probability that a non-zero value will occur during one time period. This is a minimum; overall considerations may require a longer interval.

This criterion of having one non-zero value occurring within two periods is normally met for industrial and business data if the time period is greater than or equal to one week, and a calendar month (or more practically a planning or accounting period of that order) is most typical. The number of time periods ahead for which forecasts are produced is known as the forecast horizon.

### **3.3 The moving or rolling average\***

One traditional method of forecasting the future average expected value per time period is to average the past individual values over the last n time periods. Such a moving average could be defined as

$$m_t = \frac{1}{n} \sum_{i=t-n+1}^{t} d_i$$

Or, alternatively,

$$m_t = m_{t-1} + \frac{1}{n}(d_t - d_{t-n})$$

This latter version simply means that we put the current value of the moving average as being equal to the immediate past value plus  $1/n$  times the current value less the value now  $n$  periods old.

Having calculated  $m_t$  for a stationary situation this then becomes the forecast of what one expects to occur, not only in the next time period but for any future time period.

This does not mean, however, that if one makes a forecast, say, for six months hence, this estimate cannot be modified next month, when an additional month's information can be used to improve the estimate, which is now only five months away. This concept may be slightly difficult to follow but corresponds very much with planning schedules, which are definite for the first and second months but only tentative for the third and fourth months. The tentative plans then become definite at the next two-monthly review in the same way that a vague forecast can become more definite as further information is received as time progresses.

The moving average does, however, in practice have several drawbacks which are discussed here:

- (i) Starting a moving average. When beginning the calculation moving Average from new data, because it is necessary to have individual values available for the previous  $n - 1$  periods, no true forecast can be made until at least  $n$  periods have passed.
- (ii) With a moving average, all the data included within the average are 'weighted' equally and data too old to be included are obviously given zero weighting. The weight of an item indicates the proportion of its value that an item contributes to an average, which in the case of the moving average is  $1/n$  for all items included in the average, and zero for those not included.

### SELF ASSESSMENT EXERCISE

Discuss some of the drawbacks of moving averages

A method using unequal weights could be proposed to resolve this feature, and two possible weighted averages based on either fractional or decimal concepts are shown here as equations respectively. Note that in both the sum of the weights is one; this, by definition, is always necessary of a true average.

$$m_t = \frac{1}{2}d_t + \frac{1}{4}d_{t-1} + \frac{3}{16}d_{t-2} + \frac{1}{16}d_{t-3}$$

Or

$$m_t = 0.4d_t + 0.3d_{t-1} + 0.2d_{t-2} + 0.1d_{t-3}$$

- (iii) When dealing with a moving average, the amount of past data that is retained can become excessive. A six-period moving average has been discussed but, in practice, to obtain an average which is not excessively sensitive, one can require data from up to 20 periods.
- (iv) As the sensitivity or the speed of response of a moving average is inversely proportional to n, the number of time periods included in the average, it is difficult to change this sensitivity since it is also most difficult to change the value of n, as already illustrated by the Initializing average situation.

Most of the disadvantages presented by the moving average can be overcome by a moving average of a special type in which the weighting series is exponential.

#### **4.0 CONCLUSION**

Forecasting is important in economics analysis and daily life. We often forecast changes in demand, prices, supply, exchange rates and other market situations. It is therefore important to note that forecasting is a dynamic component of our daily life.

#### **5.0 SUMMARY**

In this unit you have learn what forecasting entails, the need to forecast a stationary variable in an economic situation. You have also learned about forecasting of weighted variables.

## **6.0 TUTORED MARKED ASSIGNMENT**

What is forecasting?

Using appropriate examples discuss moving average in forecasting

## **7.0 REFERENCES/FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer, J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York.

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) Econometric Analysis, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) Introductory Econometrics, Harvard University Press.

Harvey, A.C.( 1990) The Econometrics Analysis of Time Series, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) Econometric Methods, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) Undergraduate Econometrics, John Wiley & Sons, New York,.

Hu, The-Wei (1973) Econometrics: An Introductory Analysis, University Park Press, Baltimore.

Judge, George G.,R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee(1982)Introduction to the theory and practice of Econometrics, John Wiley & Sons, New York.

Katz, David A.( 1962) *Econometric Theory and Applications*, Prentice Hall, Engle-wood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) *Textbook of Econometrics*, 2d ed., Prentice Hall, Engle-wood Cliffs, N.J.

Kmenta, Jan (1986) *Elements of Econometrics*, 2d ed., Macmillan, New York.

Maddala, G, S, (2001) *Introduction to Econometrics*, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) *Introductory Econometrics*, 2d.ed., John Wiley & Sons, New York,. A Halsted Press Book.

Madansky, A. (1976) *Foundations of Econometrics*, 2d ed., North-Holland, Amsterdam,

Mills, T.C. (1993) *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) *An Introduction to Applied Econometrics: A Time series Approach*, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) *Applied Econometrics*, Wadsworth, Belmont, California.



Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) Econometrics, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

## **UNIT 2 FORECASTING AND SEASONAL VARIATIONS**

### **CONTENTS**

1.0 INTRODUCTION

2.0 OBJECTIVES

3.0 MAIN CONTENT

3.1 Forecasting for non-stationary situations

3.2 Forecasting Techniques using Regression line

3.3 Econometric Applications

3.4 Forecasting and manpower needs

4.0 CONCLUSION

5.0 SUMMARY

6.0 TUTOR-MARKET ASSIGNMENT

7.0 REFERENCES/FURTHER READING

## **INTRODUCTION**

A linear trend is one in which the average value either increases or decreases linearly with time. A product with a linearly increasing trend could be typified by a new product with ever-increasing sales, or by a product in an expanding market retaining its percentage of that market. A product with a linearly decreasing trend could be typified by a product rapidly becoming obsolete.

## **2.0 OBJECTIVES**

At the end of this unit you should be able to:

- Discuss forecast trends.
- Explain reasons for forecasting
- Understand the applications of forecasting and manpower needs.

## **3.0 MAIN CONTENT**

### **3.1 FORECASTING AND TRENDS**

Since planning is a systematic, economic and rational way of making decisions today that will affect tomorrow, then, forecasting becomes an integral part of the planning process in any economy. There are different types of trends that are used to describe forecasting.

- (a) Seasonal trends

A seasonal trend is one in which the average varies in a cyclical fashion in sympathy with some imposed time cycle. In most practical situations, this time cycle is invariably a yearly one in which the average in some months is up, compared with the overall monthly average, and in some months is down. Fashion goods such as clothes and shoes are naturally subject to such seasonal trends, but a large section of this country's engineering industry is similarly affected via the sales of cars, which decline with the changes in seasons,

(b.) Combined linear and seasonal trends

As the name indicates, this type of trend is a direct combination of the two already mentioned. A good example of this can be seen in the bookings for airline seats. The increasing use of air transport over the years provides the linear element of the trend and the seasonal pattern of travel within each year (as influenced by peak demands during the Christmas, Easter and summer holidays) provides the seasonal element, based on an annual time cycle.

(ii) Types of trends

(A) Additive trend an additive type of trend is one in which an approximately regular amount is added to or subtracted from each consecutive average value, as influenced

by the character of the trend. For instance, with a linear additive trend an average increase in demand of ten items for each consecutive month might be expected.

(B) Ratio trends (sometimes known as multiplicative trends)

A trend of a ratio type is subject to a percentage increase or decrease, as influenced by the character of the trend. Thus, the demand for an item with an increasing linear ratio trend might be expected to increase at, say, 2 per cent per month.

(C) Combined additive and ratio trends

This type of trend, which is of course a direct combination of the two already mentioned, tends to be rather complicated to analyse mathematically and is usually dealt with as one or the other.

When describing any demand trend it is necessary to describe both its type and character. The more usual trends for which relatively simple forecasting models have been developed are:

(D) Linear additive trend

A product subject to this kind of trend would have an average value increasing (or decreasing) by an approximately fixed quantity each time period. which is distinguished from a linear ratio trend case by the fact that, although the average

value is increasing, the spread or variation of individual values about that average remains virtually constant.

### 3.1.1 Forecasting using regression line

Forecasting using the regression line equation is simply a matter of substituting the correct value of a value at time  $t$  in the regression equation

$$\hat{y}_t = a + bt$$

and evaluating the results a given expenditure data to produce a forecast for 2008 one recognizes that for that year  $t = 12$  and, hence

$$y_{12} = 366.27 + 110.09W$$

We can estimate the forecast amount by substituting for “ $w$ ” by the number in the appropriate year.

$$\begin{aligned}\hat{y}_{12} &= 366.27 + 110.09 (12) \\ &= 16687.37\end{aligned}$$

If one to adopt the normal forecasting convention, namely that the most recent observed value occurred at time  $t$  and forecasts were for  $r$  periods ahead, it follows that in equation  $t = n + \tau$ .

### 3.1.2 ECONOMETRIC APPLICATIONS

Give the following data for an economy

Estimate the regression equation and forecast the real gross domestic product using the end product year.

Gc	Pc	I	Y
4.3410	5.6809	5.2867	11.0291
4.5822	5.9086	5.4586	10.861
4.6594	5.9452	5.3721	10.833
4.6903	6.0669	5.0959	10.7541
4.6158	6.2385	4.6943	10.679
4.6921	6.3533	4.6300	10.747
4.6730	6.3720	4.8591	10.746
4.4913	6.7343	5.1270	10.713
4.8038	7.0478	5.2437	10.782
4.8736	7.1902	5.6418	10.826
4.9648	7.5048	6.0192	10.879
5.0693	7.6345	6.1136	10.9015
5.7784	8.2014	6.5384	10.906
6.1002	8.4745	6.8282	10.903
7.3645	8.6447	6.8901	10.881
7.6991	9.4423	7.1624	10.882
7.8199	9.8449	7.5021	10.900
8.0947	9.8059	7.6531	10.904
8.1124	9.9084	7.6272	10.899
7.5574	9.9195	7.5590	10.887
8.0651	9.9055	7.8922	10.915
8.0650	10.2781	7.9851	10.922
8.2117	10.6612	8.2554	10.913
8.1272	10.8766	8.7806	10.986
8.6588	10.9931	8.7526	11.062
8.8782	11.1877	8.6574	11.090
9.0998	11.3565	9.2863	11.125

9.3430	11.5929	9.4678	11.163
9.5862	11.8295	9.6493	11.196
9.8293	12.0660	9.8306	11.239
10.0723	12.3024	10.0119	11.289

The regression equation for the model can be presented in a line equation as follows:  
 using the procedure as follows, open Eviews software create a worksheet, import your set of data by browsing and clicking to upload your data to the workbook; go to quick icon on the software toolbar select estimate equation a dialogue box opens input the variable name select click ok.

Dependent Variable: Y  
 Method: Least Squares  
 Date: 02/15/16 Time: 12:53  
 Sample (adjusted): 1980 2010  
 Included observations: 31 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	10.49375	0.061958	169.3686	0.0000
GC	0.063434	0.008686	7.302817	0.0000
R-squared	0.647764	Mean dependent var		10.92944
Adjusted R-squared	0.635618	S.D. dependent var		0.154170
S.E. of regression	0.093064	Akaike info criterion		-1.848726
Sum squared resid	0.251164	Schwarz criterion		-1.756211
Log likelihood	30.65526	Hannan-Quinn criter.		-1.818569
F-statistic	53.33113	Durbin-Watson stat		0.329547
Prob(F-statistic)	0.000000			

$Y = 10.494 + 0.063GC$ . If the value of  $Y$  is given we can forecast the  $GC$  by substituting it into the equation. Assume  $GC$  is given as 24.61110. We can substitute as follows.

$$Y = 10.494 + 0.063GC$$

$$Y = 10.494 + 0.063(24.61110)$$

$$Y = 10.494 + 1.5506$$

$$Y = 12.0445$$

### **SELF ASSESSMENT EXERCISE**

Give the following data for an economy, estimate a regression equation  $Y = f(I)$  and forecast for the economy using the econometric software.

Pc	I	Y
5.6809	5.2867	11.0291
5.9086	5.4586	10.861
5.9452	5.3721	10.833
6.0669	5.0959	10.7541
6.2385	4.6943	10.679
6.3533	4.6300	10.747
6.3720	4.8591	10.746
6.7343	5.1270	10.713
7.0478	5.2437	10.782
7.1902	5.6418	10.826
7.5048	6.0192	10.879
7.6345	6.1136	10.9015
8.2014	6.5384	10.906
8.4745	6.8282	10.903
8.6447	6.8901	10.881



9.4423	7.1624	10.882
9.8449	7.5021	10.900
9.8059	7.6531	10.904
9.9084	7.6272	10.899
9.9195	7.5590	10.887
9.9055	7.8922	10.915
10.2781	7.9851	10.922
10.6612	8.2554	10.913
10.8766	8.7806	10.986
10.9931	8.7526	11.062
11.1877	8.6574	11.090
11.3565	9.2863	11.125
11.5929	9.4678	11.163
11.8295	9.6493	11.196
12.0660	9.8306	11.239
12.3024	10.0119	11.289

### 3.2 SOME AREAS OF FORECASTING

- (a) Economic development – the economic conditions of the country as well as those of the whole world will have significant effect on the operations of an organization. This will include perditions relating to Gross Domestic Product (GDP), currency strength and foreign exchange market, industrial expansion, labour market, inflation rate, interest rate, balance of payments, etc. good economic trends assist the growth of a company. On the other hand for instance, the depressions of 1929 – 1930 pay many companies out

of business. Knowledge of economic trends will assist management in making plans for its organization.

- (b) **Technological Forecasts:** these forecasts predict the new technological developments that may change the operations of an organization. The advent of the transistors put the vacuum tube totally out of business. The age of the electronic calculator totally wiped out the market for the slide rules. An aggressive entrepreneur keeps up to date with new technological developments and readily adopts new methods to improve performance of the company or business
- (c) **Competition Forecasts:** It is equally necessary to predict as what strategies your competitors will be employing to gain market share, perhaps at the cost of your market share. This is constantly happening in the airline business, electrical and electronics business. The competitor may be working to employ a different marketing strategy for a product or bringing out a substitute for the product which can be cheaper and easily acceptable by the consumers.
- (d) **Social Forecasts:** these forecasts involve predicting changes in consumer tastes, demand and attitude. Consumers have already established a trend for convenience, comforts and for products that are easy to use and easily manageable. In the 1970's, the trend was to buy small economic cars. In

the 1980's, the trend moved back to luxury and comfort. Partly, it may depend upon the general economic trends and partly on the consumer taste. Diesel cars were very popular in 1979 – 1980 and they have totally lost popularity by 1984 – 1985. Jacket, highly popular in the 1960's, is no longer fashionable today.

- (e) Other forecasts: in addition to the above major aspects, there are other critical areas with impacts on the planning process, where forecasting is equally important. These areas include the following:
- i. New laws and regulations- organizations are on a constant watch for any new laws passed relating to consumer protection or dumping of chemical wastes, and anti-trust laws. As an example, laws about truth in advertising have had a major impact on the operations of many organizations which had to make extensive changes in their operational style.
  - ii. Political Events: in politically stable countries, there may not be any dramatic political changes except that a different party in power may be more socialistic in nature, as it may interfere in private business matters. In more volatile political situations, organizations must be prepared for the worst. The cases of Kennecot Copper and ITT in Chile, during the communist takeover are classical examples of

being caught unaware. Additionally, most countries have become so interdependent that political events in one country affect the organizational events in others. The oil embargo by some Middle East countries in 1973 affected other countries consumption, demand and other market variable.

### **3.2.1 USES OF FORECASTING**

1. It improves the resource utilization example human resources, forecasting help the management of a company forecast the recruitment needs in terms of both numbers as well as the types of skills required and develop ways to avoid or correct problems before they become serious and disrupt operations.
2. It helps focus the management efforts on the most likely sources of supply. This will cut down the total costs of idle resources and reduce costs associated with market mistakes.
3. It makes provisions for replacement or back-up stock of goods from either inside or outside the organization whenever the need arises either on a temporary or permanent basis. These available sources of supply are important to identify specially in the case of any emergencies that may occur.

4. It helps achieve an integration of business plans with other operating as well as strategic plans by making available the required information base on other organizational activities.

### **SELF ASSESSMENT EXERCISE**

Discuss the necessary factors in forecasting

### **3.3 FORECASTS MANPOWER NEEDS**

Manpower forecasting is defined as the process of collecting and analysis information to determine the future supply of, and demand for, any given skill or job category. The primary purpose for manpower forecasting is to prepare for employment, training and development and proper use of human resources. Forecasting has become very important due to complexity of organizations requiring more skilled personnel which are in short supply.

In addition to assessing the current situation relevant to personnel, in the organization, an effective human resource planning program takes into consideration the future needs and trends in both job and personnel availability. This will require reliable forecasting of both the demand and supply. This will require reliable forecasting of both the demand and supply. The key to any forecasting procedure is to determine what determines the supply and demand for people, we can predict the

needs, making the planning for changes in personnel easier. Now, let us consider some salient issues here.

- a. **Opinion of expert forecasters:** Expert forecasters are those who are knowledgeable at estimating future human resource needs. These may be the personnel managers or external consultants who are asked to assess future needs. These forecasts can be taken further ahead by using the "Delphi technique", where the experts are anonymously surveyed, their opinions refined, and these opinions sent back to experts for further evaluation. The process is repeated until a consensus is reached.
- b. **Trend projection forecasts-** past trends of employee needs can be projected into the future. One method used is known as extrapolation- where, if the past trend is linear in nature, it can simply be extended into the future. For example, if in the past the company has been consistently growing, requiring on the average job addition workers per month, then by extrapolation, the future needs will be 120 workers per year.

Another method of trend projection is known as "**indexation**". This method relies upon matching employment growth with some index. For example, growth in the number of employees in the production area may be tied in with the volume of sales,

so that for a certain increase in sales, there is a corresponding increase in the number of employees in production.

Both extrapolation and indexation are simple and appropriate. However, in long range human resources projection, more sophisticated statistical analysis techniques are available and employed, taking into consideration external, organisational and workforce factors, which may not remain constant from time to time.

Some of the other forecasting methods include the ones listed below.

- (a) Budget and planning analysis- short-term human resource needs can be estimated by looking into the departmental budgets and financial avocations for more employees as well as any anticipated changes in the workforce like terminations, resignations, promotions, transfers, etc.
- (b) New ventures analysis- human resource needs for new ventures or organisational expansion can be calculated by comparison with similar operating functions. The growth of the new venture can also be established by past trends of similar operating companies.
- (c) Computer models- these are most sophisticated approaches involving solutions of mathematical formulae and equations, taking into consideration

the relationship and effect of all variables are extrapolation, indexation, survey results and other estimates.

### **SELF ASSESSMENT EXERCISE**

- 1) Discuss the key issues in manpower forecasting
- 2) Discuss some manpower forecasting techniques

### **4.0 CONCLUSION**

Forecasting is important in economics analysis and daily life. We often forecast changes in demand, prices, supply, exchange rates and other market situations. It is therefore important to note that forecasting is a dynamic component of our daily life.

### **5.0 SUMMARY**

In this unit you have learn what forecasting entails, the need to forecast a stationary and non-stationary data. We have also learn how to forecast using a regression line.

### **6.0 TUTORED MARKED ASSIGNMENT**

- 1) What is forecasting?
- 2) Discuss forecasting in stationary and non- stationary situation.



## 7.0 REFERENCES/FURTHER READING

Aigner, D. J.( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer,J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York.

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) Econometric Analysis, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) Introductory Econometrics, Harvard University Press.

Harvey, A.C. (1990) The Econometrics Analysis of Time Series, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) Econometric Methods, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) Undergraduate Econometrics, John Wiley & Sons, New York,.

Hu, The-Wei (1973) Econometrics: An Introductory Analysis, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung - Chao Lee (1982) Introduction to the theory and practice of Econometrics, John Wiley & Sons, New York.

Katz, David A. (1962) Econometric Theory and Applications, Prentice Hall, Engle-wood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) Textbook of Econometrics, 2d ed., Prentice Hall, Engle-wood Cliffs, N.J.

Kmenta, J. (1986) Elements of Econometrics, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) Introduction to Econometrics, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) *Introductory Econometrics*, 2nd.ed., John Wiley & Sons, New York,. A Halsted Press Book.

Madansky, A. (1976) *Foundations of Econometrics*, 2d ed., North-Holland, Amsterdam,

Mills, T.C. (1993) *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) *An Introduction to Applied Econometrics: A Time series Approach*, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) *Applied Econometrics*, Wadsworth, Belmont, California.

Theil, Henry (1971) *Principles of Econometrics*, John Wiley & Sons, New York.

Tintner, Gerhard (1965) *Econometrics*, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) *An Introduction to Econometrics*, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) *Econometrics*, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

## **UNIT 3 IDENTIFICATION PROBLEM**

### 1.0 INTRODUCTION

### 2..0 OBJECTIVES

### 3.0 MAIN CONTENT

#### 3.1 Meaning of Identification in Econometrics

#### 3.2 Rules for Identification

##### 3.2.1 Order Condition for Identification

##### 3.2.2 Rank Condition for Identification

#### 3.3 Identification and Choice Models

### 4.0 CONCLUSION

### 5.0 SUMMARY

### 6.0 TUTOR MARKED ASSIGNMENT

### 7.0 REFERENCES/FURTHER READING

## **1.0 INTRODUCTION**

One of the main ways of finding solution to simultaneous equation is to determine the identification of the econometric model. The identification of the model helps the researcher to focus on the method of estimating the model.

## 2.0 OBJECTIVES

At the end of this unit you should be able to:

- Discuss the concept of identification
- Discuss the Rank method of identification
- Discuss the Order method of Identification

## 3.0 MAIN CONTENT

### 3.1 MEANING OF IDENTIFICATION

Identification is a problem is a problem associated with model formulation. Identification problem arises if a given model is not correctly specified. This is sequel to the violations of the assumption that the relationship to be estimated must have a unique mathematical form. If this is violated truly, then the relationship to be estimated will contain the same variable as any other equation one is estimating. In the face unidentified model, the estimates of the parameters of the relationship between the variable measured in samples relate to the model in question or to another model or to a mixture of models.

Let us illustrate this concept of non-identifiability by making reference to a model of market equilibrium.

$$D = b_0 + b_1p + u \quad \text{(i) Demand function}$$

$$S = a_0 + a_1P + v \quad \text{(ii) Supply function}$$

$$D = S \quad \text{(iii) Clearance equation}$$

Here, we cannot identify the two models in equation (i) and (ii) since in both, quantities  $Q = f(p)$ . Hence, we may not know exactly which function one is estimating – is it the demand or the supply function?

To be sure of the function one is estimating, there is the need to examine identification to enable us judge the precise equation. To achieve this objective, we need further information on factors affecting the demand and the supply function separately (shift factors), this will help us to state clearly the function one is dealing with.

In the demand function, other determining factors such as consumers income, taste, price of other commodities, fashion, etc, should be included to differentiate this function from the supply function determined by factors such as weather, technological changes etc.

The stability of each of these functions depend, to a large extent, on the aforementioned factors.

We can state here that a model is identified if it is in unique mathematical form such that its estimates can be uniquely obtained from the given data. As a corollary, a model is not identified, its parameter estimates relate to the model in question or to another model or both. Thus, for a set of simultaneous equations, the identification of the entire set requires that the model be complete. The completeness of such models implies that it should contain at least as many independent equations as the endogenous variable.

Referring to the model of market equilibrium previously indicated, the given model is complete, because it contained 3 equations and 3 endogenous variables, D, S, and P. However, they are not identified, as previously highlighted, with reasons).

We generalize by stating that a function belonging to a system of simultaneous equation is identified, if it has a unique statistical form, meaning that there is no other equation in the system which contains the same variable as the function in question.

Thus, we can state that:

- (i) The identification of a system requires that each of the equations in the system be identified.
- (ii) The parameters of the given equation be identified (note that in the previous example, the parameters of, D ( $b_0$  and  $b_1$ ) and S, ( $a_0$ ,  $a_1$ ) cannot be statistically identified since one is not really sure of the function he is dealing with.

To establish identification, therefore, two rules are adhered to

(a) Order condition (b) Rank condition

In econometrics, there are two possible situations of identifiability of any possible situation or equation:

- (i) Under identified equation
- (ii) Identified equation

An under identified equation exists if the mathematical form of the equation is not unique. A system is under identified when one or more of its equations is not unique. A system is under identified when one or more of its equations are under identified. For such an equation or model, it is not possible to estimate all its parameters using any econometric technique.

An identified equation on the other hand has a unique statistical form. An identified equation may either come in the form of exact identification or over identified condition. A given system, therefore, is identified if all its equations are identified.

For exact identification, we estimate such model using indirect least squares. In the case of over identification, we use two stage least squares (2SLS), maximum likelihood methods.

Note that identification problem is peculiar to only those equations which contained coefficient that needs to be estimated (From the given set of data).

### **3.2 RULES (CONDITIONS) FOR IDENTIFICATION**

Identification of a model can best be established by the examination of the specification of the structural model. In applying the identification rules, we either ignore the constant term or retain it, and include in the set of variables, a dummy variable which takes the value I. In this constant, we shall ignore the constant term.

For an equation (or model) to be identified the conditions are:



## (1) The Order Condition

This condition is based on the number of variables included and those excluded from a particular equation. This is a necessary condition, although not sufficient for complete identification. This implies that the order condition for identification may be satisfied if the equation is not identified. The condition stated that: for an equation to be identified, the number of variables (endogenous and exogenous) excluded from it must be equal to or greater than the number of endogenous variables in the model less one.

Since the number of endogenous variables equal the number of equation in a complete model, the above condition may also be equivalently stated in this form: And equation is identified, if the total number of variables excluded from it but included in other equations is at least as great as the number of equations of the system less one.

Symbolically, the order condition for identification is given as:  $K - M \geq G - 1$ .

Where:  $G$  = Total number of equations (Total number of endogenous and exogenous variables)

$M$  = number of variables included in a particular equation.

So that  $K - M$  = excluded variables;  $G - 1$  = total number of equation less one.

Note that the order condition for identification is necessary for a relation to be identified but it is not sufficient for identification.

## 2 The Rank Condition

This condition maintains that in a system of  $G$  equations, any particular equation is identified if and only if it is possible to construct at least one non-zero determinant of order  $G-1$  from the coefficient of the variables excluded from that particular equation, but contained in the other equation of the model.

In order to identify a particular equation, therefore, the following steps should be followed.

- (i) Write out the parameters of all the equations of the model in a separate table, bearing in mind to assign zero to each parameter of a variable excluded from a given equation. Make a table of coefficients for each of the equations. Strike out the row of the coefficients of the equations which is being examined for identification.
- (ii) Strike out the columns in which a non-zero coefficient of the equation being examined appears. (By deleting the relevant row and columns, we are left with the coefficients of variables not in the other equations of the model).
- (iii) Form the determinant(s) of order  $(G - 1)$  and examine their values.
  - If at least one of these determinants is non-zero, the equation is identified.
  - If, however, all the determinants are zero, the equation is unidentified, and we make conclusion.
- (iv) Once the equation is identified, we then move to the order condition to determine the nature of identification.

**Example**

(1) Examine the identification state of the following model.

$$C_t = a_0 + a_1 y_t - a_2 T_t + u_t \dots\dots\dots (i)$$

$$I_t = b_0 + b_1 y_t + b_2 y_{t-1} + b_3 R_t + u_2 \dots\dots\dots (ii)$$

$$y_t = c_t + I_t + G_t \dots\dots\dots (iii)$$

**Solution**

Re-writing the above equations, we have:

$$- C_t + a_0 + a_1 y_t - a_2 T_t + u_t = 0$$

$$- I_t + b_0 + b_1 y_t + b_2 y_{t-1} + b_3 R_t + u_2 = 0$$

$$- y_t + c_t + I_t + G_t = 0$$

Equation	$C_t$	$Y_t$	$I_t$	$T_t$	$Y_{t-1}$	$R_t$	$G_t$
(i)	-1	a1	0	-a2	0	0	0
(ii)	0	b1	-1	0	b2	b3	0
(iii)	1	-1	1	0	0	0	1

- (i) To identify equation (i) delete the first row containing the coefficient of the equation and also delete the column of the table with non-zero coefficients of the equation to be identified.

Thus; we are left with.

$$\begin{array}{cccc} -1 & b_2 & b_3 & 0 \\ 1 & 0 & 0 & 1 \end{array}$$

i.e. coefficient of the excluded variables (in tabular form).

Determinant of order  $G - 1$  i.e.  $3 - 1$  are:

$$D_1 = \begin{array}{cc} -1 & b_2 \\ 1 & 0 \end{array} = b_2 \qquad D_2 = \begin{array}{cc} -1 & b_3 \\ 1 & 0 \end{array} = -b_3 \text{ etc.}$$

Since we have at least a non-zero determinant equation (i) is identified.

- For nature of identification, we use order condition as follows:

$$K - M \geq G - 1; \quad K = 7 \quad M = 3, \quad G = 3$$

$\therefore 7 - 3 > 3 - 1; 4 > 2$  (a case of over identified equation)

Using similar procedure as in (i) above equations (ii) and (iii) are respectively identified as follows:

$$\text{Coefficient of excluded variables} = -1 \quad -a_2 \quad 0$$

1 0 1 and G – determinants are:

$$D_1 = \begin{vmatrix} -1 & a_2 \\ 1 & 0 \end{vmatrix} = a_2; \quad D_2 = \begin{vmatrix} -1 & 0 \\ 1 & 1 \end{vmatrix} = -1$$

etc.

The equation (ii) is identified.

Using order condition,  $K - M \geq G - 1$ ;  $K = 7$ ,  $M = 4$ ,  $G = 3$

So that:  $7-4 > 3-1 + 3 > 2$  (over identified equation).

In equation (iii) coefficient of excluded variables are:

$$\begin{vmatrix} -a_2 & 0 & 0 \\ 0 & b_2 & b_3 \end{vmatrix}$$

So that determinant of  $G - 1$  are:

$$D_1 = \begin{vmatrix} a_2 & 0 \\ 1 & b_2 \end{vmatrix} = a_2 b_2; \quad D_2 = \begin{vmatrix} -a_2 & 0 \\ 1 & b_3 \end{vmatrix} = -a_2 b_3$$

etc.

Equation (iii) is identified.

Nature of identification is given by  $K - M \geq G - 1$ ;  $K = 7$ ,  $M = 4$ ,  $G = 3$

So that:  $7-4 > 3-1 + 3 > 2$  (over identified).

2. Consider the structural model:

$$Y_1 = 2Y_2 - x_1 + 2x_3 - x_4 + z_t + u \dots\dots\dots (i)$$

$$Y_2 = x_1 + 2Y_1 - 2X_1 - Y_t + 2x_2 + v \dots\dots\dots (ii)$$

$$Y_3 = Y_1 - Y_2 + 3Y_1 - 3x_2 - x_4 + w \dots\dots\dots (iii)$$

Where U, V and W, are error terms. Examine the identification of the model.

By re-arranging, we have:

$$-Y_1 = 2Y_2 - x_1 + 2x_3 - x_4 + z_t + u = 0 \dots\dots\dots (i)$$

$$Y_1 = y_1 - x_1 - 2x_2 + v = 0 \dots\dots\dots (ii)$$

$$4Y_1 = Y_2 - Y_3 + 3x_2 - x_4 + w = 0 \dots\dots\dots (iii)$$

Expressing the coefficients of the variables in a tabular form, we have:

<b>Equation</b>	<b>y<sub>1</sub></b>	<b>y<sub>2</sub></b>	<b>y<sub>3</sub></b>	<b>x<sub>1</sub></b>	<b>x<sub>2</sub></b>	<b>x<sub>3</sub></b>	<b>x<sub>4</sub></b>	<b>Z</b>
(i)	-1	2	0	-1	0	2	-1	1
(ii)	1	-1	0	-1	2	0	0	0
(iii)	4	-1	1-	0	-3	0	-1	0

Note: U, V and W are not variables, hence, they were excluded from the Table and subsequent computation.

Equation (i)

Coefficients of excluded variables after deleting the 1<sup>st</sup> row and columns as in example 1, are:

$$\begin{array}{cc} y_3 & x_2 \\ 0 & 2 \\ -1 & -3 \end{array}$$

∴ Determinant of order G - 1 is:

$$\begin{vmatrix} 0 & 2 \\ -1 & -3 \end{vmatrix} = 2$$

Equation (i) is identified.

- From  $K - M \geq G - 1$ ,  $K = 8, M = 6, G = 3$

∴  $8 - 6 = 3 - 1$ , that is,  $2 = 2$  (exact identification)

(ii) Coefficients of excluded variables after deleting the second row, and column with non-zero coefficients in the table are

$$\begin{array}{cccc}
 \underline{y_3} & \underline{x_3} & \underline{x_4} & \underline{Z} \\
 0 & 2 & -1 & 1 \\
 -1 & 0 & -1 & 0
 \end{array}$$

Determinants of order  $G - 1$  are

$$D_1 = \begin{vmatrix} 0 & 2 \\ -1 & 0 \end{vmatrix} = 2; \quad D_2 = \begin{vmatrix} 0 & -1 \\ -1 & -1 \end{vmatrix} = -1$$

The equation is identified.

- From  $K - M > G - 1$ ,  $K = 8, M = 4, G = 3$

$\therefore 8 - 4 > 3 - 1$ , that is,  $4 > 2$  and equation (ii) is, therefore over identified

(iii) Coefficients of excluded variable as in (i) and (ii) are:

$$\begin{array}{ccc}
 \underline{x_1} & \underline{x_3} & \underline{Z} \\
 -1 & 2 & 1 \\
 -1 & 0 & 0
 \end{array}$$

Determinants of order  $G - 1$  are

$$D_1 = \begin{vmatrix} -1 & 2 \\ -1 & 0 \end{vmatrix} = 2; \quad D_2 = \begin{vmatrix} -1 & 1 \\ -1 & 1 \end{vmatrix} = 0 \quad D_3 = \begin{vmatrix} 2 & 1 \\ 0 & 0 \end{vmatrix} = 0$$



-1 0                      -1 0                      0 0

Equation (iii) is identified.

- Using  $K - M \geq G - 1$ ,  $K = 8$ ,  $M = 5$ ,  $G = 3$  so that:  $8 - 5 > 3 - 1$ , that is,  $3 > 2$ . Therefore, equation (iii) is over identified.

### **3.3 IDENTIFICATION AND CHOICE OF ECONOMETRIC METHOD.**

Identification determines basically the choice of econometric techniques used in finding the values of the parameters of our models.

- Thus, if a relationship or model is under identified, its parameters cannot be statistically estimated by any econometric technique.
- For an exactly identified model or relationship, the most appropriate method of estimation is the indirect least squares (ILS) method.
- If an equation is over identified two stage least square (2SLS) method, or maximum likelihood method are used.

#### **Significance of Identification**

- Identification enables one to easily identify a given structural equation that is used in econometric analysis.
- It helps in the choice of estimation technique to be used in obtaining the values of the parameters.
- Identification gives the econometricians a focus. It enables him to know which of the relationships he is really dealing with.

- The nature of relationship between structural equations is revealed through identification of that model.

Correct identification gives consistent and reliable estimates

### **SELF ASSESSMENT EXERCISE**

1. Discuss identification and the choice of econometric models.
2. List the uses of Identification in economics

### **4.0 CONCLUSION**

You have learn identification in econometric models using different methods: the order condition, the rank condition and the importance of identification in applied econometrics

### **5.0 SUMMARY**

In the unit you have learn the meaning of identification and illustration on how to carry out identification of models

### **6.0 TUTOR MARKED ASSIGNMENT**

Consider the following structural model, attempt the identification of the model:

$$Y_1 = 2Y_2 - x_1 + 2x_3 - x_4 + z_t + u \dots\dots\dots (i)$$

$$Y_2 = 2x_1 + 2Y_1 - 2X_1 - Y_t + 2x_2 + v \dots\dots\dots (ii)$$

$$Y_3 = Y_1 - 2Y_2 + 3Y_1 - 3x_2 - x_4 + w \dots\dots\dots (iii)$$

## 7.0 REFERENCES/FURTHER READING

Aigner, D. J.( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer,J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York.

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) *Econometric Analysis*, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) *Introductory Econometrics*, Harvard University Press.

Harvey, A.C.( 1990) *The Econometrics Analysis of Time Series*, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G.,R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee(1982)*Introduction to the theory and practice of Econometrics*, John Wiley & Sons, New York.

Katz, David A.( 1962) *Econometric Theory and Applications*, Prentice Hall, Engle-wood Cliffs, N.J.

Klein, Lawrence R.: A (1974) *Textbook of Econometrics*, 2d ed., Prentice Hall, Engle-wood Cliffs, N.J.

Kmenta, Jan (1986) *Elements of Econometrics*, 2d ed., Macmillan, New York.

Maddala, G, S, (2001) Introduction to Econometrics, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) Introductory Econometrics, 2nd.ed., John Wiley & Sons, New York,. A Halsted Press Book.

Madansky, A. (1976) Foundations of Econometrics, 2d ed., North-Holland, Amsterdam.

Mills, T.C. (1993) The Econometric Modelling of Financial Time Series, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) Econometrics and Data Analysis for Developing Countries, Rutledge, New York.

Patterson, Kerry (2000) An Introduction to Applied Econometrics: A Time series Approach, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) Applied Econometrics, Wadsworth, Belmont, California.

Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) *Econometrics*, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) *Introductory Econometrics*, South-Western College Publishing.

## **UNIT 4 TWO STAGE LEAST SQUARE (2SLS)**

1.0 INTRODUCTION

2.0 OBJECTIVES

3.0 MAIN CONTENT

3.1 Assumptions of two stage least square

3.2 Properties of two stage least square

3.3 Merits and demerits of two stage least square

3.4 Applications of two stage least squares in model estimation

4.0 CONCLUSION

5.0 SUMMARY

6.0 TUTOR MARKED ASSIGNMENT

7.0 REFERENCES/FURTHER READING

### **1.0 INTRODUCTION**

In this unit we shall be treating the two stage least square as an econometric way of solving simultaneous equation problem. The unit shall cover the meaning the steps to take in solving two stage least square, the assumption, the properties and applications.

## **2.0 OBJECTIVES**

The main objective of this unit is to expose you to the method of two stage least square. Other specific objectives include

- Assumption of two stage least square
- Properties of two stage least square
- Applications of two stage least square in econometrics

## **3.0 MAIN CONTENT**

### **3.1 MEANING OF TWO STAGE LEAST SQUARE**

This is a single equation method. It is applied to one equation of the system at a time. Two stage least square provide satisfactory result for the estimates of the structural parameters in econometric analysis of models. 2SLS has been accepted widely as one of the most important method of the single-equation technique for estimating over-identified models. This method is applied after a proper

identification is carried out in a system of equation and clearly established that the equation is over-identified.

Two stage least square is one of the method developed to solve problems of simultaneous equation bias in econometric estimation of parameters. This method is generally an extension of indirect least square.

One of the source of simultaneous equation bias is the existence of endogenous variable in the set of exogenous variables of the econometric models. The endogenous variables have a system component determined by the pre-determined exogenous variables in the equations and a random component. The random or stochastic component creates the dependence of the relative variables with the random term of the structural equation in. simultaneous equation models. Two stage least square method generally involves the application of ordinary least square in two stages as follows:

1. Apply ordinary least squares to the reduced form equation so as to obtain estimate of the exact and random component of the endogenous variables in the equation.
2. The second stage requires that the endogenous variable appearing in the right hand side of the equation is replaced with their estimated value  $Y_t = Y_t - U_t$  and OLS is applied to the transformed original equation and obtain the



estimate of the structural parameters desired. All these can be done by the E-views software.

### **SELF ASSESMENT EXERCISE**

Discuss in full the meaning of two stage least square in econometrics.

### **3.2 ASSUMPTIONS OF TWO STAGE LEAST SQUARE**

1. According to Koutsoyannis (1977) in two stage least square the random term of the reduced form equation should satisfy the stochastic assumption of the ordinary least square. These are (a) zero mean, (b) constant variance (c) Zero-covariance. This allows the reduced form random term ( $v_i$ ) to possess the characteristic as stated above.
2. The error term of the reduced form equation ( $v_i$ ) should satisfy the OLS assumption. Beyond that it should be independent of the exogenous variables of the entire structural model.
3. The explanatory variable are not perfectly multi collinear and all macro-variables are properly and adequately aggregated.
4. It is assumed that the specification of the model is correct as far as the exogenous variable are concern. That is we assume knowledge of all the exogenous variables of the system, irrespective of the equations in which they

appear in the model. It is not necessary to know the model. It is not necessary to know the mathematical formulation of the whole system in all its ramifications. It is important to note that all the exogenous variables of the equation system are known.

5. The sample that would be used for econometric analysis is large enough. The number of observations is greater than the number of pre-determined variables in the structural equation system. If the sample size is small in comparison with the total number of the exogenous variables, it will not be possible to obtain significant estimates of the reduced coefficients when the ordinary least square is applied in the first stage.

### **SELF ASSESMENT EXERCISE**

Discuss in details the assumptions of two stage least square in econometrics.

### **3.3 PROPERTIES OF TWO STAGE LEAST SQUARE**

1. The two stage least squares estimates are asymptotically efficient under the assumptions about the distribution of the disturbances.
2. Two stage least square estimates are consistent that is their distribution collapses on the true parameter  $b$  and  $n \rightarrow \infty$
3. In large samples as  $n \rightarrow \infty$  the bias tend to zero, that is the two stage least square estimates are asymptotically unbiased. This property can be

established by deriving an explicit formula for the bias and examining the size of the bias as  $n \rightarrow \infty$

4. In two stage least squares small samples, the estimates are biased. This can be established using simple two variable model.

$$Y_1 = b_2 Y_2 + \mu$$

The transformed function becomes

$$Y_1 = b_2 \hat{Y}_2 + (U + b_2 V)$$

Where  $\hat{Y}_2 = X_1$  Now  $\hat{Y}_2$  is an exact function of  $X_1$ , which is uncorrelated with U. furthermore,  $X_1$  is by assumption uncorrelated with V. therefore  $\hat{Y}_2$  is uncorrelated with the composite random term  $(\mu + b_2 V)$ . However,  $\hat{Y}_2 = Y_2 -$

So that

$$Y_1 = b_2 (y_2 - V) + (u + b_2 V)$$

Despite the transformation, the simultaneous equation bias is not eliminated in small

### **SELF ASSESSMENT EXERCISE**

Using the necessary algebra discuss the properties of two stage least squares.

### **3.4 MERITS AND DEMERITS OF 2SLS**

1. The method of 2SLS is simple in conception and in computation using E views. It has yielded more satisfactory results than any of the other

econometric methods. It is the most important technique for the estimation of over-identified models.

2. The 2SLS method is more general than the instrument variables method, because it take into account the influence on the dependent variables of all the predetermined variables of the system, while other method choose only a small subset of predetermined variable and ignores the effects of the other exogenous variables in the model.
3. Two stage least square is adequate for the estimate of over-identified equations.
4. Two stage least squares yields consistent estimates under conditions in which ordinary least squares method face to provide result.

### **3.5 DEMERITS**

1. Two stage least square is extremely sensitive to specification errors. If we take into consideration the complexity of economic variable, consequently errors may easily emerge in the estimation process.
2. Two stage least square requires large number of observations. Models that simultaneous in nature and have small observations 2SLS may not produce efficient result.

### **SELF ASSESMENT EXERCISE**

Discuss the merits and demerits of two stage least squares

### 3.6 ECONOMETRIC APPLICATIONS

The following data represent real gross domestic product and other macroeconomic variables use two stage least squares.

Gc	Pc	I	Y
4.3410	5.6809	5.2867	11.0291
4.5822	5.9086	5.4586	10.861
4.6594	5.9452	5.3721	10.833
4.6903	6.0669	5.0959	10.7541
4.6158	6.2385	4.6943	10.679
4.6921	6.3533	4.6300	10.747
4.6730	6.3720	4.8591	10.746
4.4913	6.7343	5.1270	10.713
4.8038	7.0478	5.2437	10.782
4.8736	7.1902	5.6418	10.826
4.9648	7.5048	6.0192	10.879
5.0693	7.6345	6.1136	10.9015
5.7784	8.2014	6.5384	10.906
6.1002	8.4745	6.8282	10.903
7.3645	8.6447	6.8901	10.881
7.6991	9.4423	7.1624	10.882
7.8199	9.8449	7.5021	10.900
8.0947	9.8059	7.6531	10.904
8.1124	9.9084	7.6272	10.899
7.5574	9.9195	7.5590	10.887
8.0651	9.9055	7.8922	10.915
8.0650	10.2781	7.9851	10.922
8.2117	10.6612	8.2554	10.913
8.1272	10.8766	8.7806	10.986
8.6588	10.9931	8.7526	11.062
8.8782	11.1877	8.6574	11.090
9.0998	11.3565	9.2863	11.125
9.3430	11.5929	9.4678	11.163
9.5862	11.8295	9.6493	11.196
9.8293	12.0660	9.8306	11.239
10.0723	12.3024	10.0119	11.289

The procedure is as follows, open Eviews software create a worksheet, import your set of data by browsing and clicking to upload your data to the workbook; go to quick icon on the software toolbar input the variable name click method a dialogue box opens select “TSLS” click ok.

Dependent Variable: Y  
 Method: Two-Stage Least Squares  
 Date: 02/15/16 Time: 15:10  
 Sample (adjusted): 1980 2010  
 Included observations: 31 after adjustments  
 Instrument specification: GC PC I  
 Constant added to instrument list

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	10.37425	0.043857	236.5449	0.0000
PC	-0.126292	0.025627	-4.928163	0.0000
I	0.236791	0.032429	7.301804	0.0000
R-squared	0.877318	Mean dependent var		10.92944
Adjusted R-squared	0.868555	S.D. dependent var		0.154170
S.E. of regression	0.055895	Sum squared resid		0.087479
F-statistic	100.1164	Durbin-Watson stat		1.077134
Prob(F-statistic)	0.000000	Second-Stage SSR		0.087479
J-statistic	0.493340	Instrument rank		4
Prob(J-statistic)	0.482441			

#### INTERPRETATION

The model is a two variables personal consumption (PC) and domestic investment (I), the coefficient for personal consumption (PC) is negative (-0.126292), the coefficient domestic investment (I) is positive (0.236791). The  $R^2$  is 87% meaning

that the variables have a strong relationship. It also means that 87% of the dependent variable is explained by the independent variables of the model.

#### **4.0 CONCLUSION**

In this unit you have learned that two stage least square is the procedures for using it. You have also learned the assumptions for using the 2SLS, the properties the merits and demerits of using 2SLS.

#### **5.0 SUMMARY**

You learn the assumption, properties and applications of two stage least square in applied econometrics.

#### **6.0 TUTOR MARKED ASSIGNMENT**

- A) Using appropriate examples discuss two stage least square, stating merits and demerits.
- B) Discuss the assumptions and properties of two stage least square.
- C) Using the data given as follows attempt a two stage least square regression and explain your findings.

Expt	Impt	Gdpl	Reerl
8.9817	8.836589	11.6626	1.961753
8.91746	8.834783	11.61802	1.951143
9.102807	8.676769	11.61455	1.957894
9.105067	8.558735	11.63029	1.983491
9.208795	8.542713	11.62521	1.988381
8.907678	8.403297	11.63919	1.98704
8.292528	8.682492	11.79029	2.015485
8.351442	8.64245	11.89003	2.024691
8.27505	8.479286	11.93402	2.02152

8.598038	8.410127	11.9517	2.033946
8.580214	8.410181	12.05439	2.050844
8.742171	8.574234	12.07746	2.052809
8.56821	8.703202	12.10237	2.045245
8.265851	8.560467	12.00902	1.971508
8.373988	8.388151	12.02281	1.959423
8.423975	8.339022	12.05155	1.927216
8.567049	8.417855	12.10023	1.971276
8.730424	8.562878	12.07639	1.972203
8.576768	8.51526	12.08532	1.978637
8.387281	8.519451	12.07948	1.974604
8.510927	8.616199	12.04034	1.957368
8.610895	8.692339	12.04819	1.963174
8.672677	8.717114	12.08598	1.973266
8.718001	8.863056	12.17816	1.997212
8.770742	8.867987	12.2375	2.004407
8.87736	8.847424	12.24986	2
9.007959	8.985416	12.2703	1.99987
9.078647	9.048413	12.32556	2.002166
9.205421	9.056459	12.36109	2.005781
9.035832	9.078515	12.32485	2.01013

## 7.0 REFERENCES/FURTHER READING

Aigner, D. J.( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.



Cramer, J.S. (1969) *Empirical Econometric*, North-Holland, Amsterdam.

Davidson, James (2000). *Econometric Theory*, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) *Applied Econometrics*, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) *Introductory Econometrics*, Springer-Verlag, New York.

Dutta, M. (1975) *Econometric Methods*, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) *Econometric Analysis*, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) *Introductory Econometrics*, Harvard University Press.

Harvey, A.C. (1990) *The Econometrics Analysis of Time Series*, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York,.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee (1982) Introduction to the theory and practice of Econometrics, John Wiley & Sons, New York.

Katz, David A. (1962) Econometric Theory and Applications, Prentice Hall, Englewood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) Textbook of Econometrics, 2d ed., Prentice Hall, Englewood Cliffs, N.J.

Kmenta, Jan (1986) Elements of Econometrics, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) Introduction to Econometrics, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) Introductory Econometrics, 2d ed. John Wiley & Sons, New York, A Halsted Press Book.

Madansky, A. (1976) Foundations of Econometrics, 2d ed., North-Holland, Amsterdam.

Mills, T.C. (1993) The Econometric Modelling of Financial Time Series, Cambridge University Press.

Mukherjee, Chandan, Howard White, and Mare Wuyts (1998) Econometrics and Data Analysis for Developing Countries, Routledge, New York.

Patterson, Kerry (2000) An Introduction to Applied Econometrics: A Time series Approach, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) Applied Econometrics, Wadsworth, Belmont, California.

Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) Econometrics, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

### **MODULE 3**

Unit 1 Simultaneous Equation

Unit 2 Instrumental Variable Method (IV)

Unit 3 Full Information Likelihood Method

Unit 4 Three Stage Least Square (3SLS)

# **UNIT 1 SIMULTANEOUS EQUATION**

## **CONTENTS**

1. INTRODUCTION
2. OBJECTIVES
- 3.0 MAIN CONTENT
  - 3.1 Nature and Characteristics of Simultaneous Equation
  - 3.2 Simultaneous Equation Bias
  - 3.3 Econometric Applications
- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

## **1.0 INTRODUCTION**

These are models that exhibit two flow of influence among economic variables. It means an economic variable affects another economic variable or variables and in turn it is affected by other variables within the model. Generally in simultaneous equation models there is more than one regression equation one for each interdependent variable. This makes OLS inapplicable in estimation of equation parameters in appropriate.

## **2.0 OBJECTIVES**

At the end of this unit you should be able to:

- Know the nature and characteristics of simultaneous equation models
- Simultaneous equation bias
- Solution to simultaneous equation

### **3.0 MAIN CONTENT**

#### **3.1 Nature and Characteristics of Simultaneous Equation Models**

Models that are estimated by OLS method, emphasis is on estimating the average value of Y subject to a fixed value of X variables. The process of determining cause – effect flows from X to Y. however in simultaneous equation model, there is a two-way cause – and effect. This take place when Y is determined by X and X is also determined by Y. there is a simultaneous relationship between Y and some of the X which makes the distinction between dependent and independent variables difficult to isolate. Therefore, in simultaneous equation a set of variables are lump together and determined simultaneously by the remaining set of variables in the model. Under such a situation there is more than one equation – one for each of the mutually or jointly dependent variable in the equation system.

In simultaneous equation model estimation, the researcher cannot estimate the parameters of a single equation without considering the information provided by other equations in the model system, this is because of the joint dependence of the systems of equations. Similarly, if the equation systems are estimated using OLS by

disregarding the dependence of the equation systems the estimated variables in the model would be bias and inconsistent. As the sample size increases indefinitely the estimators do not converge to their true value.

Consider the following simple Keynesian model of income determination

$$C_t = \beta_0 + \beta_1 Y_t + \mu_1 \text{ --- (1)}$$

$$Y_t = C_t + I_t + \mu_2 \text{ --- (2)}$$

In equation (1) and (2)  $C_t$  and  $Y_t$  are mutually endogenous variables,  $U_1$  and  $U_2$  stochastic disturbance terms, the variables  $C_t$  and  $Y_t$  are both stochastic. It is therefore inconsistent to estimate the equations using OLS method.

### **SELF ASSESSMENT EXERCISE**

Discuss the characteristics of simultaneous equation models.

### **3.2 Simultaneous Equation Bias**

The methods of OLS cannot be applied to estimate single equation that is embedded in a system of simultaneous equations. If one or more of the explanatory variable are correlated with the stochastic variable in the equation due to the fact that the estimators obtained would be inconsistent.

Assume we are to estimate the parameters of the consumption function in equation (1). Assume that

$E(U_i) = 0, E(U_1^2) = \sigma^2, E(U_1 U_{i+j}) = 0$  for  $j \neq 0$  and  $\text{cor}(I_i \mu_i) = 0$  are the assumptions of the OLS regression model. It is important to show that  $Y_t$  and  $U_t$  in (2) are correlated and then prove that  $\beta_1$  is inconsistent estimator of  $\beta_1$ .

**SELF ASSESSMENT EXERCISE 2**

What is simultaneous equation bias?

**3.3 Solution to Simultaneous equation**

The correlation between  $Y_t$  and  $U_t$  can be proved as follows:

$$C_t = \mu_0 + \beta_1 Y_t + U_t$$

$$Y_t + C_t + I_t \text{-----} 4$$

Collect the terms

$$Y_t + \beta_1 Y_t = \beta_0 + I_t + U_t \text{-----} (5)$$

$$Y_t(1 - \beta_1) = \beta_0 + I_t + \mu_t \text{-----} (6)$$

$$Y_t \frac{\beta_0}{1 - \beta_1} + \frac{I}{1 - \beta_1} I_t + \frac{I}{1 - \beta_1} \mu_t \text{-----} (7)$$

$$E(Y_t) = \frac{\beta_0}{1 - \beta_1} + \frac{I}{1 - \beta_1} I_t \text{-----} (8)$$

Give that  $E(\mu_t) = 0$  and  $I_t$  is exogenous since it is fixed in advance

Subtract equation (8) from (7) we then have:

$$Y_t - E(Y_t) = \frac{\mu_t}{1 - \beta_1}$$

$$\mu_t - E(\mu_t) = \mu_t$$

$$\text{cov}(Y_t, \mu_t) = E\{Y_t - E(Y_t)\}[\mu_t - E(\mu_t)]$$

$$= \frac{E(\mu_t^2)}{1 - \beta_1}$$

$$= \frac{\sigma^2}{1 - \beta_1}$$

Because  $\delta^2$  is positive, the covariance between Y and U is different from zero. So  $Y_t$  and  $\mu_t$  are expected to be correlated which violates the assumption of the OLS that the disturbances are independent and uncorrelated with the explanatory variables (Gujarati, 2004)

### **SELF ASSESSMENT EXERCISE 3**

Using appropriate variables derive a simultaneous equation model solution.

### **4.0 CONCLUSION**

In simultaneous equation models the endogenous variable otherwise known as regress and in one equation usually appear as explanatory variable (repressor) in another equation. Because of this scenario the OLS method cannot be applied in solving the equation as estimates would become inconsistent and would not converge at their true mean.

### **5.0 TUTOR MARKED ASSIGNMENT**



Given the following hypothetical variable attempt finding a solution using the simultaneous equation method.

## **6.0 SUMMARY**

In this unit you have learn what simultaneous equation entail, simultaneous equation bias and the way to solve simultaneous equations in econometrics.

## **7.0 REFERENCES/FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C. ( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. (1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer,J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) *Introductory Econometrics*, Springer-Verlag, New York.

Dutta, M. (1975) *Econometric Methods*, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) *Econometric Analysis*, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) *Introductory Econometrics*, Harvard University Press.

Harvey, A.C.( 1990) *The Econometrics Analysis of Time Series*, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi,Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G.,R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee(1982)*Introduction to the theory and practice of Econometrics*, John Wiley & Sons, New York.

Katz, David A.( 1962) *Econometric Theory and Applications*, Prentice Hall, Engle-wood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) *Textbook of Econometrics*, 2d ed., Prentice Hall, Engle-wood Cliffs, N.J.

Kmenta, Jan (1986) *Elements of Econometrics*, 2d ed., Macmillan, New York.

Maddala, G, S, (2001) *Introduction to Econometrics*, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) *Introductory Econometrics*, 2d.ed., John Wiley & Sons, New York,. A Halsted Press Book.

Madansky, A. (1976) *Foundations of Econometrics*, 2d ed., North-Holland, Amsterdam,

Mills, T.C. (1993) *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) *An Introduction to Applied Econometrics: A Time series Approach*, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) *Applied Econometrics*, Wadsworth, Belmont, California.

Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) Econometrics, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

## **UNIT 2 INSTRUMENTAL VARIABLE METHOD**

### 1.0 INTRODUCTION

### 2.0 OBJECTIVES

### 3.0 MAIN CONTENT

#### 3.1 Outline of Instrumental Variable Method

#### 3.2 Assumptions of Instrumental Variable Method

#### 3.3 Properties of Instrumental Variable Method

### 4.0 CONCLUSION

5.0 SUMMARY

6.0 TUTOR MARKED ASSIGNMENT

7.0 REFERENCES/FURTHER READING

## **1.0 INTRODUCTION**

The instrumental variable method was developed as a solution to the problem of simultaneous equation bias. It is applicable to simultaneous equation that is over-identified. This method attains the reduction of the dependence of the stochastic variable and the explanatory variables by using the appropriate exogenous variables as the instruments in model estimation. The model estimates using instrumental variable method are consistent when large samples are used though inconsistent if small samples are used for estimation of simultaneous equation models.

## **2.0 OBJECTIVES**

At the end of this unit you should be able to:

- ❖ Discuss the instrumental variable as an alternative method of regression
- ❖ Use the econometric software to estimate equations using the instrumental variable method.

## **3.0 MAIN CONTENT**

### **3.1 OUTLINE OF INSTRUMENTAL VARIABLE**

1. The researcher should choose the appropriate instrumental variables that will replace the endogenous variables that appear as explanatory variables in the model.

The instrumental variable is an exogenous variable that is within the system of simultaneous equation system. Such a variable should meet the following condition.

- a. It should be strongly correlated with the dependent variable that it will replace in the structural simultaneous equation system.
  - b. Instrumental variable should be truly exogenous hence uncorrelated with the stochastic variable (a) in the structural equation.
  - c. The instrumental variable should be correlated with exogenous variable already existing in the set of explanatory variables of the particular structural equation.
  - d. When more than one instrumental variable is to be used in the same structural equation. They must be the least correlated with each other, this is to avoid the problem of multicollinearity
2. Multiply the structural equation through by the exogenous variables already existing in it. Since these predetermined variables are their own instruments and sum the equation over all sample observation. This procedure will provide as many linear equation as there are unknown parameters. From the solution

of these equations the estimates of the structural parameters are obtained (Koutsoyannis 2977).

### **SELF ASSESSMENT EXERCISE 1**

Attempt an outline of the procedures of using the instrumental variable method in econometric analysis

### **3.2 ASSUMPTIONS OF INSTRUMENTAL VARIABLE**

The instrumental variable method uses the transformed OLS equation to provide solution to simultaneous equation problem. The instrumental variable method requires the multiplication of each of the OLS equation by an instrumental variable determine the solution that is appropriate for the model equation. The assumptions of the instrumental variable include the following.

1. The researcher should have a complete knowledge of some exogenous variables in other equations of the complete system that can be used as instruments in model estimation.
2. The new random term  $ZU$  should satisfy the ordinary least square assumption of asymptotic behavior.
3. The exogenous variable that is the instrumental variable used in estimation should not be perfectly multicollinearity.
4. The structural function should be identified for it to be used effectively in estimation.

5. There should be proper aggregation of functional variables.

The instrumental variable method obeys the assumption of the OLS method in addition to the additional assumptions stated above.

## **SELF ASSESSMENT EXERCISE 2**

Discuss the assumptions of the instrumental variable method.

### **3.3 PROPERTIES OF THE INSTRUMENTAL VARIABLE**

1. When the sample used for research are small, the estimates of model equation by instrumental variable will be biased.
2. Estimation of model equation with instrumental variable method using large sample size the estimates would be consistent. However, for an estimate to be asymptotically consistent there are two conditions that should be met:
  - a. The estimate should be asymptotically unbiased.
  - b. The distribution of the values of the estimate should collapse on the true  $\beta$ , that is it should be centered on the true structural parameter.
3. The estimates of instrumental variable method are inefficient. It means that the estimates do not pose minimum variance when compared with estimates obtained from other economic techniques of model estimation.

### **Merits and Demerits of Instrumental variable Method**

1. Instrumental variable method is a help to us to estimate models that are of simultaneous equation system.



2. Instrumental variable method provides a good alternative method of model estimation if the data is well aggregated.
3. Instrumental variable method gives a better result when data is quarterly and the sample size is very large.

The demerits of instrumental variable method include the following:

1. The method of instrumental variable takes into account only part of the influence of the exogenous variables on the dependent variable. This is because the method includes only a certain exogenous variable and omission of other variables.
2. The selection of instrument in the estimation process is arbitrary. Therefore, the values of the estimates will differ depending on the choice of the model instrumental variable.
3. In practical estimation, the endogenous variable is related to more than one exogenous variable. The choice of a variable as the optimal instrument is quite challenging.

In this unit, you have learned that instrumental variable method of simultaneous equation method. You have also been take through the subject matter from concept to the outline of instrumental variables, assumptions, principles, merits and demerits of instrumental variable method.

### **SELF ASSESSMENT EXERCISE 3**

Discuss the properties, merits and demerits of the instrumental variable method.

#### **4.0 CONCLUSION**

This unit have help you to know the instrumental variable method of econometric analysis, you have learn the assumptions, properties of the instrumental variable method

#### **5.0 SUMMARY**

In this unit you have learn about the instrumental variable as another econometric method of estimating equations. This method requires that you can identify the required instruments when estimating the equations.

#### **6.0 TUTOR MARKED ASSIGNMENT**

Explain in details the concept of instrumental variables, the Assumptions, the properties and the merits of the instrumental variables method.

#### **7.0 REFERENCES/FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) *Econometric Models and Methods*, John Wiley & Sons, New York.

Cramer,J.S, (1969) *Empirical Econometric*, North-Holland, Amsterdam.

Davidson, James (2000). *Econometric Theory*, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) *Applied Econometrics*, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) *Introductory Econometrics*, Springer-Verlag, New York.

Dutta, M. (1975) *Econometric Methods*, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) *Econometric Analysis*, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) *Introductory Econometrics*, Harvard University Press.

Harvey, A.C.( 1990) *The Econometrics Analysis of Time Series*, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York,.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee (1982) *Introduction to the theory and practice of Econometrics*, John Wiley & Sons, New York.

Katz, David A. (1962) *Econometric Theory and Applications*, Prentice Hall, Englewood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) *Textbook of Econometrics*, 2d ed., Prentice Hall, Englewood Cliffs, N.J.

Kmenta, Jan (1986) *Elements of Econometrics*, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) *Introduction to Econometrics*, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) *Introductory Econometrics*, 2d ed., John Wiley & Sons, New York, A Halsted Press Book.

Madansky, A. (1976) *Foundations of Econometrics*, 2d ed., North-Holland, Amsterdam,

Mills, T.C. (1993) *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Mukherjee, Chandan, Howard White, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) An Introduction to Applied Econometrics: A Time series Approach, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) Applied Econometrics, Wadsworth, Belmont, California.

Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) Econometrics, 2d ed., John Wiley & Sons, New York.

Wooldridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

### **UNIT 3 FULL INFORMATION MAXIMUM LIKELIHOOD METHOD (FIML)**

#### **1. INTRODUCTION**

#### **2. OBJECTIVES**

#### **3.0 MAIN CONTENT**

##### **3.1 Estimation Procedure**

##### **3.2 Properties and Assumptions of Full Information Likelihood**

##### **3.3 Applied Estimation**

- 4.0 CONCLUSION
- 5.0 SUMMARY
- 6.0 TUTOR MARKED ASSIGNMENT
- 7.0 REFERENCES/FURTHER READING

## **1.0 INTRODUCTION**

According to Kontsoyiannis (1977) full information maximum likelihood is a system method that is this method is applied to all the equations of the model and yields estimates of all the structural parameters contemporaneously. It is a straight forward extension of the maximum likelihood. In FIML it is assumed that the complete specification of all the equations of the model is known. Similarly the random variables of the structural equations are normally distributed with zero means. The random terms of the different equations are not intercorrelated. When they are independent their covariance will be zero.

## **3.0 MAIN CONTENT**

### **3.1 THE ESTIMATION PROCEDURE**

1. Formulation of the likelihood function for the random variables of all the equations and for all sample values. Given the sample of size  $n$ , for each structural equation we have a set of  $n$  values for its random variable.

2. Estimation of the Jacobian is the determinant for the error terms of all structural equations. The Jacobian is the determinant of partial derivatives of the transformation function solved for stochastic variable with respect to the endogenous variable.
3. Application of the transformation rule so as to obtain the likelihood function of the endogenous variable ( $Y_1 - -Y_G$ ) from the likelihood function of the random terms ( $\mu_1, \mu_2 \mu_G$ )
4. Estimation of the partial derivatives of the likelihood function with respect to the structural parameters and the variances of all (G) random terms
5. Equating of the partial derivatives of the likelihood function to zero and solution of the resulting system of equations for the unknown structural parameters and the variances of the random terms.
6. Estimation of the standard errors, variances of the parameter estimates.

### **SELF ASSESSMENT EXERCISE 1**

Outline the estimation procedures of full information likelihood method

#### **3.2 PROPERTIES OF FIML**

1. When the research samples are small, full information likelihood method yield estimates that are biased.
2. If the research samples is large, full information likelihood method estimates possess the property of efficiency.

3. When the research sample is large FIML Method estimates are consistent.

### **3.2.1 ASSUMPTIONS OF FULL INFORMATION LIKELIHOOD**

The basic assumptions of the full information likelihood method of Econometric estimates is as follows:

1. The full information likelihood assumes full information full knowledge of the complete specification of all the equations in the model. Information about the variables appearing in the model and the mathematical form of all the equation are well known to the researcher.
2. Full information likelihood assumes that the random disturbances of the various equations of the model are normally distributed with zero means and constant variances.
3. There should be the independence of the random terms of the various equations that is adopted.
4. FIML assumes that the model is recursive

### **SELF ASSESSMENT EXERCISE 2**

Discuss the properties and the assumptions of full information likelihood method in econometric analysis.

#### **Merits of FIML**

1. Estimates of full information maximum likelihood possesses the characteristics of Efficiency.



2. Full information maximum likelihood estimates are consistent.

### **Demerits of FIML**

1. Estimates of full information maximum likelihood are biased for small samples.
2. The requirement of complete knowledge of the complete specification of the model is usually unattainable.
3. The method is cumbersome because of estimating equations which are nonlinear in the parameters, it is an expensive method in data, time and money.
4. The method is sensitive to specification errors compared with other methods.

### **SELF ASSESSMENT EXERCISE 3**

Discuss the merits and demerits of full information likelihood method

#### **Illustration**

The data given below is derived from the performance of an economy.

Estimate an equation using full information likelihood method.

Gc	Pc	I	Y
4.3410	5.6809	5.2867	11.0291
4.5822	5.9086	5.4586	10.861
4.6594	5.9452	5.3721	10.833

4.6903	6.0669	5.0959	10.7541
4.6158	6.2385	4.6943	10.679
4.6921	6.3533	4.6300	10.747
4.6730	6.3720	4.8591	10.746
4.4913	6.7343	5.1270	10.713
4.8038	7.0478	5.2437	10.782
4.8736	7.1902	5.6418	10.826
4.9648	7.5048	6.0192	10.879
5.0693	7.6345	6.1136	10.9015
5.7784	8.2014	6.5384	10.906
6.1002	8.4745	6.8282	10.903
7.3645	8.6447	6.8901	10.881
7.6991	9.4423	7.1624	10.882
7.8199	9.8449	7.5021	10.900
8.0947	9.8059	7.6531	10.904
8.1124	9.9084	7.6272	10.899
7.5574	9.9195	7.5590	10.887
8.0651	9.9055	7.8922	10.915
8.0650	10.2781	7.9851	10.922
8.2117	10.6612	8.2554	10.913
8.1272	10.8766	8.7806	10.986
8.6588	10.9931	8.7526	11.062
8.8782	11.1877	8.6574	11.090
9.0998	11.3565	9.2863	11.125
9.3430	11.5929	9.4678	11.163
9.5862	11.8295	9.6493	11.196
9.8293	12.0660	9.8306	11.239
10.0723	12.3024	10.0119	11.289

The procedure is as follows, open Eviews software create a worksheet, import your set of data by browsing and clicking to upload your data to the workbook; go to quick icon on the software toolbar input the variable name click method a dialogue box opens select "LILM" click ok.

Dependent Variable: Y

Method: LIML / K-Class  
 Date: 02/15/16 Time: 15:13  
 Sample (adjusted): 1980 2010  
 Included observations: 31 after adjustments  
 Covariance type: IV  
 Instrument specification: GC PC  
 Constant added to instrument list

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	10.38855	0.053305	194.8895	0.0000
I	0.157200	0.129927	1.209912	0.2364
PC	-0.064487	0.101029	-0.638301	0.5285
R-squared	0.850926	Mean dependent var		10.92944
Adjusted R-squared	0.840277	S.D. dependent var		0.154170
S.E. of regression	0.061615	Sum squared resid		0.106298
Durbin-Watson stat	0.673200	LIML min. eigenvalue		1.000000

## SELF ASSESSMENT EXERCISE 4

Attempt a regression analysis using full information likelihood method with data above

### 4.0 SUMMARY

In this unit you have learn about the full information likelihood method the basic assumptions, the properties of the full information likelihood method, the illustration on how to estimate equations using full information likelihood method.

### 5.0 CONCLUSION

In this unit you have learn what is full information maximum likelihood method, the estimation procedure, the properties and assumptions of the full information maximum likelihood method.

## **6.0 TUTOR MARKED ASSIGNMENT**

1 Carefully discuss the full information likelihood method of estimation in econometric analysis.

2 Given the following information about a hypothetical economy, estimate a regression equation using variables of your choice as instruments and regressors.

## **REFERENCES/FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer, J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). *Econometric Theory*, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) *Applied Econometrics*, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) *Introductory Econometrics*, Springer-Verlag, New York.

Dutta, M. (1975) *Econometric Methods*, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) *Econometric Analysis*, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) *Introductory Econometrics*, Harvard University Press.

Harvey, A.C.( 1990) *The Econometrics Analysis of Time Series*, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York,.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsoung-Chao Lee (1982) Introduction to the theory and practice of Econometrics, John Wiley & Sons, New York.

Katz, David A. (1962) Econometric Theory and Applications, Prentice Hall, Englewood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) Textbook of Econometrics, 2d ed., Prentice Hall, Englewood Cliffs, N.J.

Kmenta, Jan (1986) Elements of Econometrics, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) Introduction to Econometrics, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) Introductory Econometrics, 2d ed., John Wiley & Sons, New York, A Halsted Press Book.

Madansky, A. (1976) Foundations of Econometrics, 2d ed., North-Holland, Amsterdam,

Mills, T.C. (1993) The Econometric Modelling of Financial Time Series, Cambridge University Press.

Mukherjee, Chandan, Howard White, and Mare Wuyts (1998) Econometrics and Data Analysis for Developing Countries, Routledge, New York.

Patterson, Kerry (2000) An Introduction to Applied Econometrics: A Time series Approach, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) Applied Econometrics, Wadsworth, Belmont, California.

Theil, Henry (1971) Principles of Econometrics, John Wiley & Sons, New York.

Tintner, Gerhard (1965) Econometrics, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) An Introduction to Econometrics, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) Econometrics, 2d ed., John Wiley & Sons, New York.

Wooldbridge, Jeffrey M. (2000) Introductory Econometrics, South-Western College Publishing.

Wooldridge, J. M. (2009) Introductory Econometrics A modern Approach, Cengage Learning Singapore 4<sup>th</sup> Edition.

## **UNIT 4    THREE STAGE LEAST SQUARES (3SLS)**

### **1.0    INTRODUCTION**

## 2.0 OBJECTIVES

## 3.0 MAIN CONTENT

3.1 Assumption of Three Stage Least Square

3.2 Properties of Three Stage Least Square

3.3 The Three Stage Estimation Method

## 4.0 CONCLUSION

## 5.0 SUMMARY

## 6.0 TUTOR MARKED ASSIGNMENT

## 7.0 REFERENCES/FURTHER READING

### **1.0 INTRODUCTION**

In this unit you will learn the meaning of three stage least square, the assumptions the stages of determining three stage least square. The process is very simple but you are required to go through the topic several times in order to have good knowledge of the three stage least square.

### **2.0 OBJECTIVE**

The objective of this unit are

- Know the meaning of three stage least square
- Discuss the assumptions and method of three stage estimation
- Learn the practical applications with on hand practical on eviews

### **3.0 MAIN CONTENT**



### **3.1 THE MEANING OF THREE STAGE LEAST SQUARE**

Three stage least square (3SLS) is an Econometric method of estimation that is applied to all equations in the model at the same time and gives estimates of all the equation estimate of parameters simultaneously. It is an extension of two stage least square. Three stage least square involves the application of least square in three successive stages. It uses more information than the single equation methods, by taking into account the entire model structure with all restrictions that the structure imposes on the values of the equation parameters.

Usually single equation technique make only of the variables appearing in the entire model, but ignore the restrictions set by the structure on the coefficients of other equations as well as the contemporaneous dependence of the random terms of the various equations (Koutsoyannis 1977). The random term of any equation  $\mu_i$  in simultaneous equation model is correlated with the error term of other equations.

#### **3.1 Assumptions of Three Stage Least Square**

1. The model equation system is complete and correctly specified in all variables. This means the variables that appear in the model are completely know and their mathematical form well specified
2. The error term of each equation is not serially correlated. The model specified should be free of autocorrelation.

3. The random variables of the various relations of the system are contemporaneously dependent.

Based on the nature of economic phenomena and the simplifications of economic models the random variables become contemporaneously correlated.  $E(\mu_i/\mu_j) \neq 0$ . Because of restrictions we include variables that are most important while those that are less useful in the model are taken care of by the random variable in the equation. When some variables are omitted from more relations of the equation system it become inevitable that the random variable of these relations are correlated that is why the application 3SLS becomes more appropriate.

5. The equation system is over-identified. When there are under-identified equations in the system, they can be made identifiable by changing their specification or they can be dropped from the system of equation. Similarly indentifies and definitional equations can be dropped after using them to Eliminated the relevant variables from the equation system.

## SELF ASSESSMENT EXERCISE 1

Carefully discuss the assumptions of the three stage least square in econometric analysis

### **3.2 PROPERTIES OF THREE STAGE ESTIMATES**

1. The estimates of three stage least square are biased but consistent.

2. Estimates of 3SLS are efficient. This is because more information is used in estimating
3. 3SLS requires complete knowledge of the specification of the entire model.
4. 3SLS estimation process requires a large amount of data
5. 3SLS is sensitive to specification errors in the equation system. A single specification error can affect all the equations in the model.

Though 3SLS is appropriate for econometric estimation of equation system, it is time consuming and tedious

## **SELF ASSESSMENT EXERCISE 2**

Outline the properties of three stage least square

### **3.3 THE THREE STAGES OF ESTIMATION**

The first stage is to estimate the reduced – form of all the equations of the system. This allow us to know the value of all the dependent variables in the system.

$$Y_1 = f(X_1, X_2 \dots X_n)$$

$$Y_2 = f(X_1, X_2 \dots X_n)$$

$$Y_z = f(X_1, X_2 \dots X_n)$$

The first stage enables us to estimate the values of the endogenous variable  $\hat{Y}_1, \hat{Y}_2, \hat{Y}_z$

Stage Two

The calculated values of the endogenous variables in stage one are substituted in the right hand side of the structural equation and apply least squares to the transformed

equations. This give us the 2SLS of all the b's and Ys which are used for the estimation of the error terms of the various equations in the model. We then find the set of Z errors.

$$l_1, l_2, l_3 \dots l_Z$$

Each corresponding to the error term ( $\mu$ ) of the respective structural equation in the model.

The variance and covariance of the estimated error terms can be computed using the formula.

$$\sigma_{e_1 e_2} = \frac{\sum_{ii} e_{21}}{n} \quad \sigma_{\ell_1 \ell_2} = \frac{\sum_{ii} \ell_{2i}}{n}$$

$$\sigma_{e_1 e_3} = \frac{\sum_{ii} e_{31}}{n} \quad \sigma_{\ell_1 \ell_3} = \frac{\sum_{ii} \ell_{3i}}{n}$$

### Stage three

The variances and covariance of the error terms are used to obtain the transformation of the initial variables for the application of the generalized least square.

### SELF ASSESSMENT EXERCISE 3

Using algebraic method discuss the three stage least square

#### **4.0 SUMMARY**

In this unit you have learn about the three stage least square method the basic assumptions, the properties of the three stage least square method, the illustration on how to estimate equations using three stage least square method.

#### **5.0 CONCLUSION**

In this unit you have learn what is three stage least square method, the estimation procedure, the properties and assumptions of the three stage least square method.

#### **6.0 TUTOR MARKED ASSIGNMENT**

- A) State the basic steps for the econometric analysis using the three stage least square method
- B) Given the following data, using appropriate variables compute a regression equation using three stage least square.

#### **7.0 REFERENCES/FURTHER READING**

Aigner, D. J,( 1971) Basic Econometrics, Prentice Hall, Englewood Cliffs, N.J.

Berndt, Ernst R.(1991) The practice of Econometrics: Classic and contemporary, Addison-Wesley.

Bridge, J.I.( 1971) Applied Econometrics, North-Holland, Amsterdam.

Chow, Gregory C.( 1983) Econometric Methods, McGraw-Hill, New York.

Christ, C.F. ( 1966) Econometric Models and Methods, John Wiley & Sons, New York.

Cramer,J.S, (1969) Empirical Econometric, North-Holland, Amsterdam.

Davidson, James (2000). Econometric Theory, Blackwell Publishers, Oxford, U.K.

Desail, Meghnad. (1969) Applied Econometrics, McGraw-Hill, New York,

Dhrymes, Phoebus J. (1978) Introductory Econometrics, Springer-Verlag, New York.

Dutta, M. (1975) Econometric Methods, South-Western Publishing Company, Cincinnati.

Greene, William H. (2000) Econometric Analysis, 4<sup>th</sup> ed., Prentice Hall, Engle-wood cliffs, N. J.

Goldberger, Arthur S. (1998) Introductory Econometrics, Harvard University Press.

Harvey, A.C.( 1990) The Econometrics Analysis of Time Series, 2d ed., MIT Press, Cambridge, Massachusetts.

Hayashi, Fumio (1984) *Econometric Methods*, 3d ed., McGraw-Hill, New York.

Hill, Carter, William Griffiths, and George Judge (2001) *Undergraduate Econometrics*, John Wiley & Sons, New York,.

Hu, The-Wei (1973) *Econometrics: An Introductory Analysis*, University Park Press, Baltimore.

Judge, George G., R. Carter Hill, William E. Griffiths, Helmut Lutkepohl, and Tsung-Chao Lee (1982) *Introduction to the theory and practice of Econometrics*, John Wiley & Sons, New York.

Katz, David A. (1962) *Econometric Theory and Applications*, Prentice Hall, Engle-wood Cliffs, N.J.,

Klein, Lawrence R.: A (1974) *Textbook of Econometrics*, 2d ed., Prentice Hall, Engle-wood Cliffs, N.J.

Kmenta, Jan (1986) *Elements of Econometrics*, 2d ed., Macmillan, New York.

Maddala, G. S. (2001) *Introduction to Econometrics*, John Wiley & Sons, 3d ed., New York.

Mark, Stewart B., and Kenneth F. Wallis (1981) *Introductory Econometrics*, 2d ed., John Wiley & Sons, New York, A Halsted Press Book.

Madansky, A. (1976) *Foundations of Econometrics*, 2d ed., North-Holland, Amsterdam,

Mills, T.C. (1993) *The Econometric Modelling of Financial Time Series*, Cambridge University Press.

Mukherjee, Chandan, Howard white, and Mare Wuyts (1998) *Econometrics and Data Analysis for Developing Countries*, Routledge, New York.

Patterson, Kerry (2000) *An Introduction to Applied Econometrics: A Time series Approach*, St. Martin's Press, New York.

Rao, Potluri, and Roger leRoy Miller (1971) *Applied Econometrics*, Wadsworth, Belmont, California.

Theil, Henry (1971) *Principles of Econometrics*, John Wiley & Sons, New York.

Tintner, Gerhard (1965) *Econometrics*, John Wiley & Sons (Science ed.), New York.

Walters, A.A, (1968) *An Introduction to Econometrics*, Macmillan, London.

Wonnacott, R.J., and T. H. Wonnacott (1979) *Econometrics*, 2d ed., John Wiley & Sons, New York.

Wooldbridge, Jeffrey M. (2000) *Introductory Econometrics*, South-Western College Publishing.